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Phil. Trans. R. Soc. B 2013 368, 20120046, published online 21 January 2013

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# How multiple mating by females affects sexual selection 

Stephen M. Shuster, William R. Briggs and Patricia A. Dennis

Department of Biological Sciences, Northern Arizona University, Flagstaff, AZ 86011-5640, USA

## Research

Cite this article: Shuster SM, Briggs WR, Dennis PA. 2013 How multiple mating by females affects sexual selection.
Phil Trans R Soc B 368: 20120046.
http://dx.doi.org/10.1098/rstb.2012.0046

One contribution of 14 to a Theme Issue 'The polyandry revolution'.

## Subject Areas:

evolution, theoretical biology, behaviour

## Keywords:

polyandrous mating, sperm competition, post-mating sexual selection, opportunity for sexual selection, female life-history, cryptic female choice

## Author for correspondence:

Stephen M. Shuster
e-mail: stephen.shuster@nau.edu


#### Abstract

Multiple mating by females is widely thought to encourage post-mating sexual selection and enhance female fitness. We show that whether polyandrous mating has these effects depends on two conditions. Condition 1 is the pattern of sperm utilization by females; specifically, whether, among females, male mating number, $m$ (i.e. the number of times a male mates with one or more females) covaries with male offspring number, $o$. Polyandrous mating enhances sexual selection only when males who are successful at multiple mating also sire most or all of each of their mates' offspring, i.e. only when $\operatorname{Cov}_{O^{\prime}}(m, o)$, is positive. Condition 2 is the pattern of female reproductive life-history; specifically, whether female mating number, $m$, covaries with female offspring number, $o$. Only semelparity does not erode sexual selection, whereas iteroparity (i.e. when $\operatorname{Cov}_{q}(m, 0)$, is positive) always increases the variance in offspring numbers among females, which always decreases the intensity of sexual selection on males. To document the covariance between mating number and offspring number for each sex, it is necessary to assign progeny to all parents, as well as identify mating and non-mating individuals. To document significant fitness gains by females through iteroparity, it is necessary to determine the relative magnitudes of male as well as female contributions to the total variance in relative fitness. We show how such data can be collected, how often they are collected, and we explain the circumstances in which selection favouring multiple mating by females can be strong or weak.


## 1. Introduction

We have three goals in writing this article: (i) to identify the circumstances in which multiple mating by females influences post-mating sexual selection; (ii) to describe how these circumstances can be most effectively measured; and (iii) to document how often current researchers actually collect these data. In the context of our paper, we define sexual selection as a sex difference in the variance in relative fitness resulting from differential parentage among the individuals of one sex [1]. Our definition follows Darwin [2, p. 205] in focusing on 'the advantage certain individuals have over others of the same sex and species in exclusive relation to reproduction'.

We begin by reviewing the current literature on how multiple mating by females is thought to affect male fitness variance in the context of post-mating sexual selection. We next describe the condition necessary for post-mating sexual selection to occur, in particular, whether the pattern of sperm utilization by females allows male mating number, $m$ (i.e. the number of times a male mates with one or more females; the average mating number is known as 'mating number promiscuity' ([1]; see $\S 1 c(i v))$ to covary with male offspring number, $o$. We argue that polyandrous mating enhances sexual selection only when males who are successful at multiple mating also sire most or all of each of their mates' offspring, i.e. only when $\operatorname{Cov}_{0^{\prime}}(m, 0)$, is positive. We describe the parameters necessary to quantify the pattern of sperm utilization by females, and using a worked example, we explain how this condition affects the strength of post-mating sexual selection on males. We then summarize in tabular form how often these results are reported in the current literature. Our review focuses on gonochoristic animals because sexual selection, when it exists, is likely to be stronger and is less complicated
to quantify in these species [1,3]. However, we illustrate our method for quantifying the opportunity for post-mating sexual selection using an excellent dataset from hermaphroditic snails [4], because this study is one of the few sufficiently detailed to contain the parameters we require.

We next review the current literature on how the pattern of female reproductive life-history, i.e. the number of times females mate and produce offspring, is thought to affect female fitness variance. Although multiple mating by females is widely thought to enhance female fitness indirectly (i.e. through enhanced offspring fitness), we argue that the direct fitness benefits females gain from polyandrous mating are sufficient to explain this behaviour. We explain that polyandrous mating by females enhances female fitness only when females who mate repeatedly produce the most offspring, i.e. when the covariance between female mating number, $m$, and offspring number, $o, \operatorname{Cov}_{\rho}(m, o)$, is positive. We describe the parameters necessary to document this covariance, as well as how simultaneously considering its effects in both sexes provides a means for understanding when post-mating sexual selection will be strong or weak. We explain how variation in female life-history can enhance or diminish the strength of sexual selection, and we describe how such variance may be partitioned and explored experimentally. We summarize in tabular form how often these results for females are reported in the current literature, and lastly, we explain how well the data for females, as well as those for males, coincide with current views of post-mating sexual selection and polyandrous mating.

Overall, we find the widespread perception that multiple mating by females can simultaneously encourage sexual selection in males, as well as enhance female fitness, is unsupported; these are usually mutually exclusive conditions. Furthermore, we show that although multiple mating may be common, direct, quantitative evidence of post-mating sexual selection is surprisingly scarce (i.e. the necessary positive covariance between mating number and fertilization success among males, $\left.\operatorname{Cov}_{0^{( }(m, 0),}[1,5]\right)$, in most cases, is either unmeasured or does not exist. We also show that post-mating sexual selection, occurring by sperm competition and/or cryptic female choice (see §2a), is seldom accurately measured because most studies do not include non-mating males in their estimates of selection, or simply fail to measure selection at all. The majority of researchers focus instead on the predicted outcomes of an evolutionary history of sperm competition or, less often, on measurements of fitness variance within the class of mating males, the class usually representing the smaller of the two sources of the total variance in male offspring numbers (figure 1). While numerous studies report fitness gains accrued by females who mate repeatedly, the scale of these gains remains unknown because their relative contribution to total selection's strength is undocumented. Our goal is not to find fault with existing studies; the body of this literature is impressive in size, scope and detail. Rather, we seek to reveal where additional studies could more effectively substantiate, or more convincingly refute, the hypothesis that post-mating sexual selection is ubiquitous and strong [6-8]. We hope that our findings may stimulate re-analysis of past studies, as well as inspire future studies of multiple mating and post-mating sexual selection that emphasize the quantification of the actual evolutionary processes shaping male and female phenotypes.


Figure 1. Partitioning the variance in offspring numbers for a simulated population of 100 males and 100 females as the proportion of non-mating individuals in the population, $p_{0}$, increases using equation (2.3); in this population the mean and variance in offspring numbers are randomly distributed (mean $\pm$ s.d. $=5 \pm 2.23$ ); note that as $p_{0}$ increases, the fraction of the total variance in offspring numbers, $V_{\text {total, }}$, that lies among the classes of mating and non-mating males, $V_{\text {among }} / V_{\text {total }}$ (solid line), steadily increases.

## 2. Sexual selection and the pattern of sperm utilization by females

## (a) Current literature

Sperm competition and cryptic female choice are recognized as significant sources of male fitness variance in a wide diversity of taxa (reviews in [3-10]). These two processes are presumed to be distinct; in sperm competition, male ejaculates or sperm vie for fertilization, either within or outside the female's body, whereas in cryptic female choice, females encourage or disfavour particular sperm or ejaculates in accomplishing syngamy, again either within or outside the female reproductive tract. In fact, the fitness outcomes of each process for males are identical, and are measurable in the same way, specifically, by identifying, at the population level, whether males who are successful in fertilizing ova represent a subset of the males who successfully mate. Because these processes at present are quantitatively indistinguishable, we will refer to the fitness outcomes of both sperm competition and cryptic female choice under the general heading of 'post-mating sexual selection'.

Existing studies of post-mating sexual selection are of six types including: (i) positive correlations between particular male traits and male mating or fertilization success (although in most cases these results are obtained from experiments in which each female in the experimental population is allowed to mate with only two males, who each mate with no other females, followed by a search by researchers for patterns in fertilization success within the sample of experimental threesomes; e.g. last male mating precedence [8,11,12]); (ii) positive correlations between particular sperm traits and male fertilization success, again generally using pairs of males for each experimental female as described above [6-8,13-17]; (iii) positive correlations between testis mass or ejaculate volume and the presumed or experimentally manipulated level of sperm competition (reviews in
[18-21]; (iv) evidence of differential insemination success or ejaculate retention induced within particular females by particular males [22]; and (v) evidence of mixed paternity within the clutches of individual females [23-25]. Until recently, relatively few studies have attempted to measure (vi) the variance in relative fitness arising from post-mating competition among males, or among hermaphroditic individuals emphasizing male function (i.e. the opportunity for sexual selection [4,26-31]). These and other results are summarized in table 1.

Only studies of type (vi) constitute direct, quantitative evidence of post-mating sexual selection because they measure either the opportunity for sexual selection [1], or selection intensity acting directly on mate numbers (via Bateman gradients, [94,95]) or on traits such as body size ([3,4,31]; see also $\S 2 b$ ). However, even in this last category, most studies summarized in table 1 use genetic paternity data to document the existence of multiple mating or to measure the variance in offspring numbers within the class of successfully mating males (but see $[4,94]$ ). While indicating the potential for post-mating sexual selection, as shown in figure 1, such estimates tend either to overestimate or underestimate the variance in male fitness, sometimes severely [96]. Thus, while indirect or correlational evidence of post-mating sexual selection is abundant, such studies can imply the existence of strong sexual selection when such selection is actually weak (less than $2 \%$ of total selection [94]). Without direct, quantitative evidence of the magnitude of post-mating sexual selection intensity at the population level, understanding of this phenomenon must be considered incomplete.

## (b) Direct evidence of post-mating sexual selection

As Darwin [2] first observed, in order for sexual selection to occur, certain males within a population must experience proportionate reproductive success. Concomitantly, when some males are disproportionately successful in siring offspring, other males must be excluded from siring any offspring at all $[1,96]$. This same principle holds for postmating sexual selection. Thus, among the males who are successful at mating, some males must be disproportionately successful at fertilizing ova. This condition requires that certain successfully mating males are unsuccessful at fertilizing any ova at all [1]. Stated differently, in order for sexual selection to intensify by either sperm competition or cryptic female choice, male fitness variance post-mating must exceed that which exists pre-mating. If the reverse condition is true, post-mating processes will tend to reduce the intensity of sexual selection overall.

Abundant evidence suggests that within individual females, particular males' sperm do experience differential fertilization success [97-99]. However, these circumstances are not always sufficient to generate measurable sexual selection within a population. We assert that to reach the conclusion that post-mating sexual selection occurs, researchers must obtain three kinds of data. First, to demonstrate the existence of such sexual selection, it is necessary to document the proportions of males within a population (not simply between pairs of males (cf. [8,13-17])) who are successful, as well as males who are unsuccessful, in siring offspring [1]. This is necessary because the variance in male fitness consists of two components: the variance in fitness within the class of successful males, and the variance in fitness between the classes of successful and unsuccessful males [26,27]. As
sexual selection intensifies, the latter component of fitness variance represents the larger of the two components of total selection (figure 1). Documentation of only the fitness of males who successfully fertilize ova does not permit the estimation of the between-male (also called the amongmale) component of fitness [100]. Similarly, studies involving pairs of males who each mate with a particular female, but do not mate with any other females [13-17], do not provide a means for estimating the among-male component of fitness variance; such results reveal only the relative success of the two males who mate with a particular female. While the results obtained from experimental threesomes may be replicated within an experiment, and while they may elegantly simulate the common phenomenon among insects of sperm displacement, wherein the last male to mate removes or inactivates nearly all of the sperm of previously mating males [69], even robust replication of this method within an experiment cannot reveal the relative fertilization success that any one male within the research population experiences, relative to other males mating with different females within the same population (but see [31]). Such experiments, like those focusing only on successful males, do not reveal the subset of males who successfully mate, yet fail to fertilize ova within the population of mated females. As a result, such results cannot reveal the actual magnitude of postmating sexual selection in nature.

Second, in order to document the existence of disproportionate fertilization success among the mating males, it is necessary to document the magnitude and sign of the covariance between mating number, $m$, and offspring number, $o$, among males $\left(\operatorname{Cov}_{0^{0}}(m, 0)\right)$ [1,101], as well as the magnitude and sign of the covariance between mating number, $m$, and offspring number, $o$, among females, $\operatorname{Cov}_{p}(m, o)$ (see $\S 3 c(i i)$ ). Estimating this covariance for males is necessary because, as stated above, multiple mating by females enhances sexual selection only when a subset of the successfully mating males are differentially successful in siring young. Estimating this covariance for females is necessary as well because multiple mating by females enhances female fitness only when this covariance is positive [1]. Moreover, a sex difference in the sign of this covariance provides a quantitative measure of sexual conflict, as well as explicit predictions about the relative propensities of each sex to seek or not to seek multiple mating, independent of sex differences in gametic investment [101]. Different mating systems can influence the magnitude and sign of this covariance for both sexes. Thus, understanding the possible outcomes of these covariances provides a means for predicting when post-mating sexual selection can be strong or weak.

Third, to determine how much of total sexual selection can be attributed to post-mating competition among the ejaculates of successfully mating males, it is necessary to (i) identify the fraction of males who fail to mate, as well as the fraction of males who mate successfully but fail to sire offspring; (ii) document the mean and variance in offspring numbers for males and females; (iii) partition total sexual selection into its pre- and post-mating components; (iv) document the total opportunity for selection on males and females; and (v) estimate the sex difference in the opportunity for selection (i.e. the opportunity for sexual selection $[1,26,101,102]$ ). These steps are necessary because, although post-mating sexual selection is generally assumed to be strong, the actual strength of such selection relative to
Table 1. Existing studies of indicating post-mating sexual selection.

x





Table 1. (Continued.)


toads
(Bufo bufo) [70]
Reptiles
adder
(Vipera berus) [71]
(Podocnemis
unifilis) [72]
common lizard
(Laecerta vivipara) [73]
green turtles
(Chelonia mydas) [74]
water snakes
(Nerodia sipedon) [75]
tuatara
(Sphenodon
punctatus) [76]
water snakes
(Nerodia sipedon) [77]
coal til
(Parus ater) [78]
unnocks
modularis) [79]
Table 1. (Continued.)




 competition positive correlation
between sperm
traits and mating
or fertilization
success (pairs of
males per female) positive correlation
> positive correlation
between male traits and mating or fertilization
> success (pairs of
> males per female)
dwarf mongoose
(Helogale
parvula) [90]
golden lion tamarin
(Leontopithecus
rosalia) [91]
wood mice
(Apodemus
sylvaticus) [24]
striped field mouse
(Apodemus
agrarius) [92]
wood mice
(A. sylvaticus) [92]
wood mice
(A. sylvaticus) [93]
selection in other contexts has rarely been measured. Where it has been measured, the strength of such selection appears to be small (less than 2\% [31]).

## (c) Identifying the appropriate parameters for males

## (i) Fundamental parameters

If the parentage of all offspring produced in each generation can be accurately assigned, estimation of all of the parameters mentioned above is straightforward. Methods for estimating the proportions of mating and non-mating individuals within each sex, $p_{\mathrm{S}}$, and $p_{0}$, respectively (where $\left[p_{\mathrm{S}}+p_{0}\right]=1$ ), are available in [1], as are methods for estimating the average and variance in offspring numbers for each sex, $O$ and $V_{\mathrm{O}}$, respectively, as well as the opportunity for selection within each sex, as $I=V_{\mathrm{O}} / O^{2}$.
(ii) Variance in male fitness and the opportunity for

## sexual selection

Wade [26] showed that when males differ in mate numbers, the total variance in male offspring numbers can be determined if the mean and variance in offspring numbers for females, $O_{Q}$, and $V_{\mathrm{O} Q}$, are known. This is true because the average number of offspring per male equals $R O_{q}$, where $R$ is the average number of mates per male, $N_{\rho} / N_{O^{7}}$ (i.e. the sex ratio (cf. [1])). Also, the total variance in male fitness, in terms of offspring numbers, $V_{\text {Oơtotal }}$, can be partitioned into two components, $V_{\text {Oơwithin, }}$ the average of the variances in offspring number within the classes of mating males, and $V_{\mathrm{O} \text { oramong }^{\prime} \text {, the variance in the average number of offspring }}$ between the mating and non-mating male classes, such that $V_{\mathrm{O} \text { Ototal }^{\prime}}=V_{\mathrm{O} \text { Orwithin }^{\prime}}+V_{\mathrm{OO} \text { 'between }}$. As shown elsewhere [ $1,26,102$ ], when the total variance in male fitness is divided by the squared average in male fitness, $\left(R O_{\ell}\right)^{2}$, the opportunity for selection on males, $I_{0^{7}}$, equals the opportunity for selection on females, $I_{q}$, adjusted by the sex ratio, $R$, plus the opportunity for selection due to differences in mate numbers among males, $I_{\text {mates }}\left(=I_{\mathrm{s}}[27,103]\right)$, or $I_{\mathrm{O}^{7}}=1 / R\left(I_{\mathrm{C}}\right)+$ $I_{\text {mates }}$. When the sex ratio, $R$, equals unity, this expression can be rearranged to show that $I_{0^{7}}-I_{q}=I_{\text {mates }}$.

The opportunity for sexual selection thus equals the sex difference in the opportunity for selection $[1,26,27]$. Strong sexual selection indicates that variance in relative fitness for males, $I_{0^{3}}$, is greater than the variance in relative fitness for females, $I_{\rho}$. Similarly, when the variance in relative fitness for females increases, it comes at the expense of sexual selection (a relationship that is not clear in [103] because the opportunity for selection in each sex is called $I_{\mathrm{s}}$ ). To account for conventional and sex role-reversed species, Shuster \& Wade [2] called the sex difference in the opportunity for selection $\Delta \mathrm{I}$, which is positive in species with conventional sex roles, and negative in species that are sex-role reversed.

## (iii) The opportunity for post-mating sexual selection

With accurate paternity assignment, the fraction of mating males can be further subdivided to reveal the opportunity for selection due to the effects of post-mating sexual selection. When considering only successful and unsuccessful males, Wade \& Shuster $[104,105]$ showed that the total variance in male fitness can be partitioned into two quantities, the
variance in fitness within the class of individuals who successfully reproduce, $V_{\text {O }^{7} \text { within, }}$ and the variance in fitness between the successfully and unsuccessfully reproducing classes, $V_{\text {O'between }}$.

When members of the male population can be identified as belonging to successful, $p_{\mathrm{SO}^{7}}$, and unsuccessful, $p_{00^{7}}$, classes (where $p_{\mathrm{So}^{\prime}}=\left[1-p_{0 o^{\circ}}\right]$ ), and when the variance in offspring numbers among the successful males, $V_{\mathrm{OO}^{\prime},}$ is known, the within-group variance in male fitness, $V_{\text {Oơwithin, }}$ is equal to the average of the variance in fitness for each of the reproducing classes; that is, the variance in fitness for each class weighted by its population frequency. Since there are only two classes, successful and unsuccessful, this expression can be written as
$V_{\mathrm{O} 0^{7} \text { within }}=\left(p_{0 O^{\pi^{\prime}}}\right)(0)+\left(p_{\mathrm{Sơ}^{7}}\right) V_{\mathrm{OO}^{7}}=\left(p_{\mathrm{SO}^{\pi}}\right) V_{\mathrm{OO}^{7}}$,
where $V_{\mathrm{O}^{\circ}}$ is the variance in offspring numbers among the males who secure mates.

When the average in offspring numbers among the successful males, $\mathrm{O}_{0^{\prime}}$, is known, the component of the variance in male fitness that exists between the classes of successfully and unsuccessfully reproducing individuals, $V_{\text {Oơbetween, }}$ is equal to the difference in the average number of offspring between the two classes, squared, or $\left(O_{0^{7}}-0\right)^{2}$, multiplied by the variance between the fitness categories, $\left(p_{0 O^{\prime}}\right)(1-$ $p_{00^{\circ}}$ ), or
$V_{\text {OO'between }}=\mathrm{O}_{\mathrm{O}^{\top}}^{2}\left(p_{0 \circlearrowleft^{\top}}\right)\left(p_{\mathrm{So}^{\top}}\right)$.
The total variance in male fitness in terms of offspring numbers, $V_{\text {Oơtotal }}$, is the sum of these two variance components, or
$V_{\mathrm{O} O^{7} \text { total }}=\left(p_{\mathrm{SO}^{3}}\right) V_{\mathrm{OO}^{7}}+O_{\mathrm{O}^{7}}^{2}\left(p_{0 \sigma^{7}}\right)\left(p_{\mathrm{SO}^{\pi}}\right)$.
Consider again that when post-mating sexual selection occurs, the male population consists of not just two, but three fractions: (i) the fraction of males that fails to mate, $p_{00^{3}}$, (ii) the fraction of males that mates but fails to sire offspring, $p_{\text {Sm0 }}{ }^{\text {o }}$ and (iii) the fraction of males that mates and sires offspring because they possess competitive or preferred sperm, $p_{\mathrm{So}^{7}}$. Each of these fractions of the population sum to unity, or
$p_{0 \sigma^{7}}+p_{\mathrm{Sm} 00^{\pi}}+p_{\mathrm{Sơ}^{\pi}}=1$.
If we first use ( $p_{0 \sigma^{7}}+p_{\mathrm{Sm0o}^{7}}$ ) to estimate the unsuccessful fraction of the male population, $p_{00^{7}}$, in equation (2.3), we obtain the total variance in fitness in terms of offspring numbers for the reproducing and non-reproducing males, $V_{\text {Oơtotal }}$. Rewritten, equation (2.3) now equals
$V_{\mathrm{OO}^{7} \text { total }}=\left(p_{\mathrm{SO}_{\mathrm{O}^{\pi}}}\right) V_{\mathrm{OO}^{\pi}}+O_{\mathrm{O}^{7}}^{2}\left(p_{0 \mathrm{O}^{7}}+p_{\mathrm{Sm} 0 O^{\pi}}\right)\left(p_{\mathrm{SO}_{\mathrm{O}^{\pi}}}\right)$.
If we next use only $p_{00^{\circ}}$ [instead of $\left.\left(p_{00^{7}}+p_{\text {Sm0 }}{ }^{\circ}\right)\right]$ to estimate the unsuccessful fraction of the male population in equation (2.3), we obtain the variance in male fitness that is due to all sources of selection except that which is caused by differences among mating males in their ability to sire young. We call this fraction, the variance in male mating success due to pre-mating fitness components, $V_{\mathrm{Oo}^{\text {p }}}$ pre. The total variance in male fitness is equal to the sum of pre-mating and post-mating fitness components, or


Table 2. Estimating the opportunity for selection due to pre-mating and post-mating sexual selection in hermaphroditic freshwater snails (P. acuta) using equations (2.1)-(2.7) and data from Pélissié et al. [4]; parameters explained in text; asterisk (*) values for $I_{s}$ match those reported in [4], indicating that our estimates of the mean and the variance in cMS and gMS from [4] for each sexual function are correct.

## males

females

| parameter |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| M (cMS) | 2.13 |  | 2.13 |  |
| $V_{M}$ | 0.66 |  | 0.94 |  |
| ${ }^{*} I_{\text {s }}$ | 0.15 |  | 0.21 |  |
| 0 (gMS) | 1.48 |  | 1.47 |  |
| $V_{0}$ | 0.80 |  | 0.77 |  |
| ${ }^{*} I_{\text {s }}$ | 0.37 |  | 0.36 |  |
| $p_{0}$ | 0.03 |  | 0.05 |  |
| $p_{\text {sm0 }}$ | 0.16 |  | 0.14 |  |
| $p_{\text {s }}$ | 0.82 |  | 0.81 |  |
| $V_{\text {ototal }}=\left(p_{s}\right) V_{0}+0^{2}\left(p_{0}+p_{\text {smo }}\right)\left(p_{s}\right)$ |  |  |  |  |
| $V_{\text {Owithin }}$ | 0.65 |  | 0.62 |  |
| $V_{\text {Oamong }}$ | 0.33 |  | 0.33 |  |
| $V_{\text {Ototal }}$ | 0.98 |  | 0.95 |  |
| $V_{\text {Opre }}=\left(p_{s}\right) V_{0}+0^{2}\left(p_{0}\right)\left(p_{s}\right)$ |  |  |  |  |
| $V_{\text {Owithin }}$ | 0.65 |  | 0.62 |  |
| $V_{\text {Oamong }}$ | 0.04 |  | 0.09 |  |
| $V_{\text {Ototal }}$ | 0.70 |  | 0.71 |  |
| $V_{\text {Opost }}=V_{\text {Ototal }}-V_{\text {Opre }}$ |  | \% of $I_{\text {total }}$ |  | \% of $I_{\text {total }}$ |
| $V_{\text {Owithin }}$ | 0.98 |  | 0.95 |  |
| $V_{\text {Oamong }}$ | 0.70 |  | 0.71 |  |
| $V_{\text {Ototal }}$ | 0.28 |  | 0.25 |  |
| $I_{\text {total }}$ | 0.45 |  | 0.44 |  |
| 1 pre | 0.32 | 71 | 0.33 | 74 |
| $I_{\text {post }}$ | 0.13 | 29 | 0.11 | 26 |

By subtracting $V_{\text {Oơpre }}$ from both sides of equation (2.6), we have,
$V_{\text {OƠppost }}=V_{\text {Oơtotal }}-V_{\text {Oởpre }}$,
wherein $V_{\text {Oơppost }^{\prime}}$ equals the variance in male fitness that is due to the effects of post-mating sexual selection. By dividing equation (2.7) by the squared average fitness for males, $\mathrm{O}_{\mathbf{O}^{2}}^{2}$, we obtain the opportunity for selection among males that is due to post-mating sexual selection, $I_{O^{7} \text { post }}=I_{\mathrm{OO}^{7} \text { total }}-I_{\mathrm{OO}^{7} \text { pre. }}$. The relative contribution of postmating sexual selection to other sources of selection can then be expressed as the ratio of these parameters. For example, the fraction of the total opportunity for selection on males due to post-mating sexual selection can be estimated as $I_{O^{\text {P p post }}} / I_{\text {O't total } \text {. }}$

A recent dataset obtained from hermaphroditic snails, Physa acuta, provides a worked example for this approach: Pélissié et al. [4] report the mating success (cMS) and the reproductive success (gMS) for 120 snails mating and producing offspring via male and female function. Using their figure 1, we identified all of the variables mentioned in equation (2.5) for individuals reproducing as functional males and as functional females (table 2). Although we did not estimate all of the variables mentioned in [4], we verified
our estimates of the mean and variance in mating numbers and offspring numbers, and the opportunity for selection for both sexes from their table. When we partitioned the total variance in fitness into the fitness components identified in equations (2.1)-(2.7) for each sex, the total variance in relative fitness ( $I_{\text {total }}$ ) equalled 0.45 and 0.44 for males and females, respectively. Using equation (2.7), we found the proportion of the total variance in relative fitness due to postmating sexual selection equal to 0.29 and 0.26 for males and females, respectively (table 2). The lack of confidence limits for the results in [4], as well as in ours, limits the conclusions possible from both analyses. However, our results are consistent with the conclusions of the authors in [4] who argue that pre-mating sexual selection is stronger than post-mating sexual selection in this species.
(iv) The covariance between mating numbers and offspring numbers for males
The covariance between male mating number and the number of offspring sired by males equals
$\operatorname{Cov}_{\circlearrowleft^{7}}(m, o)=\left(\frac{\Sigma\left[m_{i} o_{i}\right]}{N_{O^{\top}}}\right)-\left(O_{O^{3}}\right)\left(P_{O^{\prime}}\right)$,
where $m_{i} o_{i}$ is the product of individual mating number and offspring number for each $i$ th male; here, mating number, $m$, is the number of matings per male counting each mating, whether with the same or with a different partner, as a single event. $N_{0^{\pi}}$ is the total number of males, $O_{0^{\pi}}$ is the average number of offspring per male and $P_{0^{\prime}}$ is the average male mating number promiscuity, i.e. the average number of matings per male $[1,101]$. Whether $\operatorname{Cov}_{\sigma^{7}}(m, 0)$ is positive, negative or zero can be understood by considering whether winners in post-mating sexual selection fertilize all, none or a random number of progeny with each of their mates. Although this expression may appear unfamiliar, estimates of the covariance between mate numbers and offspring numbers have a long history; this expression equals the numerator of the standardized covariance between mate numbers and offspring numbers, also known as the Bateman gradient [4,94,95,103].

When 'winners fertilize all' (WFA) [1] or even fertilize most of their mate's offspring, $\operatorname{Cov}_{0^{\prime}}(m, o)$ is positive and post-mating sexual selection is likely because only particular mating males are successful in siring young. Although other males may be successful in mating, their sperm are outcompeted by or are less attractive than those of successful males; thus only a subset of the mating males are successful in producing offspring [5].

When male fertilization success is randomly distributed across females ('winners fertilize some', WFS [1], $\operatorname{Cov}_{0^{\prime}}(m, o)$ is zero, and post-mating sexual selection (particularly sperm competition) works much like a lottery, wherein male success overall is randomly distributed but males who allocate the most sperm to individual females are likely to be most successful in siring offspring [8,10]. Again, clustered ejaculates and sperm competition may exist, but the number of ejaculates each male assigns to a particular female, or whether individual males are able to limit the number of other ejaculates a given female receives, is what determines a male's overall success. Post-mating sexual selection is possible in such situations, but only to the degree that males are able to deliver disproportionate volumes of sperm to multiple females.

The common assumption is that males are able to produce as much sperm as is necessary to accomplish this task [106], but examples of sperm limitation for both sexes are remarkably common, given the importance of large sperm volumes to sperm competition by fair or loaded lottery [8]. Most outcrossing plants and broadcast-spawning animals routinely experience pollen or sperm limitation, causing sexual selection to be relatively weak $[1,107]$. Moreover, sperm limitation in species in which males may breed often is documented in a wide range of species, including nematodes, fruitflies, crabs, birds and sheep (review in [108]). Models of sperm competition [8] routinely assume a tradeoff between the number of mates males obtain and the number of sperm they allocate per mate, such that males must 'optimize' ejaculate size or sperm number. The more limited individual males are in their ability to transfer large volumes of sperm or ejaculate to multiple females, the weaker post-mating sexual selection must be.

When males sire most or all the offspring of one of their mates, but sire few or no offspring with their other mates ('winners fertilize one', WFO), $\operatorname{Cov}_{0^{\prime}}(m, o)$ is negative, and post-mating sexual selection is impossible. Here, the success of each male depends on the female with whom he mates
and fertilization success tends to be equitably distributed among males. Although ejaculates may be clustered within certain females, and although sperm competition or cryptic female choice may be responsible for the tendency for one male to sire the offspring of each female, a negative covariance indicates that no single male is more successful among females than another, i.e. post-mating sexual selection is nil [49,98]. This pattern of sperm utilization is typical of situations interpreted as 'genetic complementarity $[109,110]$ '.
(d) Measuring the appropriate parameters for males

Table 1 summarizes the current literature claiming to document post-mating sexual selection resulting from multiple mating by females. While the development of molecular techniques that allow the assignment of parentage has made estimating the above parameters easier [10,111,112], several persistent problems remain even with the most accurate assignments of parentage to offspring. In particular, documenting the existence of multiple paternity within broods is not equivalent to documenting the existence of fitness variance among males, the condition necessary to establish post-mating sexual selection. Although genetic markers detected multiple sires within families in 64 per cent of the studies reported ( $47 / 74$, table 1), such markers were often insufficiently variable to allow unambiguous paternity assignment except under the most controlled experimental conditions. Exclusion analyses usually allow neither the number of successful males, $p_{\mathrm{SO}^{3}}$, nor the number of unsuccessful males in a population, $p_{00^{3}}$, to be accurately identified ( $[85,113,114]$, table 1 ); thus only 15 per cent of the 74 studies documented $p_{00^{7}}$ (table 1). In some cases, attempts at paternity assignment simply failed, in cases where certain progeny were not assigned to any of the males within the genotyped population [ $47,65,87,88,93,115$ ].

This does not mean that incomplete estimates of parentage are useless; it simply means that the power of inference for such studies decreases as the proportion of unidentified parents and offspring increases. When data are available on the average number of males per male or per female ( $H=$ harem size), the proportion of non-mating males within the population, $p_{00^{7}}$, can be estimated using the equation, $p_{00^{7}}=1-(R / H)$, wherein $R$ equals the sex ratio [101]. However, in general, the current limitations of genetic paternity data prevent accurate estimates of the proportions of mating and non-mating males within the population. Perhaps not surprisingly, estimates of $I_{0^{r}}$ and $I_{\text {mates }}$ (i.e. $I_{\mathrm{s}}$ vis [103]) are few, and only about one-third of studies report results indicating or inferring the sign of $\operatorname{Cov}_{\sigma^{( }}(m, 0)(28 / 74$; table 1). However, consistent with our predictions, among these studies, male traits associated with sperm competition appear in $11 / 14$ studies in which $\operatorname{Cov}_{0^{\prime}}(m, o)$ is positive, whereas no such traits are reported in 10/14 studies in which $\operatorname{Cov}_{O^{( }}(m, 0)$ is zero or negative (Fisher's exact test, $p=0.021$; table 1).

## 3. Sexual selection and the pattern of female life-history

## (a) Current literature

Multiple mating by females is widely thought to enhance female fitness, either directly, by increasing the number of
offspring females produce [116-120], or indirectly, by allowing females to increase the survivorship of their offspring via genes or resources they receive from males [85,87,88,121,122]. While multiple mating by females has been shown in diverse taxa to enhance female fitness directly ( $30-70 \%$ in 122 species [119]), indirect benefits females gain from multiple mating are less clear because of confusion about the data necessary to document this effect

Results to date suggest that direct effects on female fitness are impressively large (table 3). Primarily for this reason, we choose here to consider only the direct fitness benefits females may gain from mates and mating. As noted by Arnqvist \& Nilsson [119], direct effects of female fitness appear so pervasive that presumed indirect effects on female fitness are unnecessary to account for the widespread occurrence of polyandrous mating. However, our choice is also substantiated by Wolf \& Wade [134], who identified additional reasons why indirect effects on female fitness gained through offspring are likely to have weak, inconsistent or intractable effects on parental fitness. These authors note that because offspring are related to each parent only by one-half, selection on parental genes affecting offspring fitness is only half as strong as selection on zygotically expressed genes with the same fitness effects [135]. Thus, assigning offspring fitness directly to parents can overestimate the evolutionary outcome of 'good genes' or other resources that offspring may receive from parents. Conditional or sex-limited exposure of such genes to selection during mate choice or parental care can weaken indirect selection still further, and further exaggerate the evolutionary importance of 'genetic quality'.

Wolf \& Wade [134] also argued that while offspring survival may indirectly influence parental fitness, offspring survival directly influences offspring fitness. Because offspring fitness belongs to offspring themselves, assigning offspring fitness to parents without experimentally disentangling parental and offspring influences on total fitness confounds these estimates across generations, leading to erroneous evolutionary inferences about how parental traits may respond to selection. Furthermore, because parental and offspring traits are often genetically correlated, selection may act on these traits via pleiotropy, linkage or non-random mating in unpredictable ways, particularly if genetic correlations are negative, as they often are [134]. Without advance knowledge of the genetic variance/covariance structure of maternal and offspring traits, as well as the influences these traits have on the relative fitnesses of parents and offspring, it is impossible to predict how selection on offspring performance may influence maternal phenotype. For these reasons, we exclude from this review articles that identify fitness benefits to polyandrously mating females in any terms other than offspring numbers.

## (b) Direct evidence of fitness advantages to multiple mating by females

Why is it important to consider the effects of multiple mating on female fitness when considering sexual selection? The short explanation is that increases in the variance in fitness among females tend to erode the opportunity for sexual selection on males [100]. As explained in [1], when a female mates once and produces only one clutch of offspring, she assigns her entire reproductive output to a single male.

When a female mates more than once, she divides her clutch into several sub-clutches, equal in number to the number of sires. The production of multiple clutches either by multiple mating or iteroparity increases the variance in female fitness, and it allows more males to mate. Both changes decrease the variance in fitness among males and so decrease the opportunity for sexual selection [1].

What constitutes direct evidence that females increase their fitness by multiple mating, and what evidence exists that such gains influence sexual selection on males? While abundant evidence exists that multiple mating by females may enhance female fitness directly, few studies have placed their results within an evolutionary context except by inference. Furthermore, while theoretical evidence exists that multiple mating may reduce the intensity of sexual selection [1,100], few examples of this effect are known [1,86,136]. We assert therefore that three kinds of data are required to argue that selection favours multiple mating by females.

First, to demonstrate the existence of significant variance in female fitness associated with multiple mating, it is necessary to document the proportion of females in the population who are unsuccessful in producing offspring [ 1,96 ]. This is necessary because, just as in males, the variance in female fitness consists of two components: the variance in fitness within the class of successfully reproducing females, and the variance in fitness between the successful and unsuccessful females [26]. As reproduction becomes increasingly disproportionate among females, the latter component of fitness variance represents the larger fraction of the two components of total selection (figure 1). The larger the fraction of total fitness female fitness represents, the more sexual selection is weakened [26,27].

Second, to demonstrate the existence of differential reproduction by females due to differences in mate numbers, it is necessary to document the magnitude and sign of the covariance between mating number, $m$, and offspring number, $o$, among females, or $\operatorname{Cov}_{q}(m, o)$. If this covariance is positive, it indicates that multiple mating by females enhances female fitness, with the magnitude of the covariance proportional to the strength of such selection. This condition is necessary for multiple mating by females to enhance female fitness. However, another important reason to document whether or not multiple mating by females enhances offspring numbers is that, depending on the sign and magnitude of the covariance between mating number and offspring number for males, $\operatorname{Cov}_{0^{2}}(m, 0)$, the sign and magnitude of $\operatorname{Cov}_{\rho}(m, o)$ for females mating with such males can lead to mating system dynamics not predicted by considering each of these covariances separately, or by not considering these covariances at all (see $\S 3 c($ iii )).

Third, to determine whether the fitness advantages females gain by multiple mating are likely to lead to significant evolutionary change, it is necessary to scale these potential fitness benefits to the total opportunity for selection on females, as well as to the total opportunity for selection on both sexes (methods in [1]). To examine the opportunity for selection on females, $I_{Q}$, it is necessary to partition the total
 (i) the variance in fitness due to the effects of different clutch sizes among females, (ii) the variance in female fitness due to the effects of matings with different males, and (iii) the variance in female fitness due to the effects of different numbers of clutches per female [1]. These components of the

Table 3. (Continued.)

| taxon/common name (species) | parasite avoidance | harassment prevention | predation avoidance | replenish sperm | increased life span | variance components of female life-history |  |  |  |  | $p_{0}$ ¢ | $\mathrm{Cov}_{\mathrm{q}}(\mathrm{m}, 0)$ | $I_{\text {¢ }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | $V_{\text {cuutches }}$ | $V_{\text {c,dutch }}$ | $V_{\text {cs,sires }}$ | $V_{\text {cs, } \text { cmales }}$ | $V_{\text {muliplemates }}$ |  |  |  |
| cabbage beetles <br> (Colaphellus bowringi) [127] |  |  |  |  | (-) |  |  |  |  |  |  | (-) |  |
| seed beetle <br> (Stator limbatus) [43] |  |  |  |  |  |  |  |  |  |  |  | (+) |  |
| red flour beetle (Tribolium castaneum) [42] |  |  |  |  | $\times$ |  |  |  |  | x |  | (-) |  |
| flour beetles <br> (Tribolium castaneum) [41] |  |  |  |  |  |  |  |  |  |  |  | (-) |  |
| mealworm beetles (Tenebrio molitor) [128] |  |  |  | x |  |  |  |  |  | x |  | (+) |  |
| armyworms <br> (Pseudaletia unipuncta) [129] |  |  |  |  | (+) |  |  |  | x | x |  | (+) |  |
| almond moth (Cadra cutella) [130] |  |  |  |  | (-) |  |  |  |  |  |  | (-) |  |
| seaweed fly (Coelopa frigida) [46] |  |  |  |  |  |  |  |  |  |  |  | (+) |  |
| fruitfies <br> (Orosophila melanogaster) [88] |  |  |  |  |  |  |  |  |  |  |  | (-) |  |
| fruitflies <br> (D. melanogaster) [49] |  |  |  |  |  |  |  |  |  |  |  | (-) |  |
| fruitflies <br> (D. melanogaster) [50] |  |  |  |  |  | * | x | x | x | x | * | 0 |  |
| fruitflies <br> (D. melanogaster) [51] |  |  |  |  |  | $\times$ |  |  |  | $\times$ |  | 0 | x |
| fruitflies (Drosophila viriliss [51] |  |  |  |  |  | $\times$ |  |  |  | x |  | 0 | x |
| fruitilies (Drosophila lummei) [51] |  |  |  |  |  | x |  |  |  | x |  | 0 | x |
| fruitflies <br> (Drosophila bifurca) [51] |  |  |  |  |  | x |  |  |  | x |  | 0 | x |

Table 3. (Continued.)
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$+$

Table 3. (Continued.)

variance in fitness for females can be converted to opportunities for selection by dividing each by the squared average in female fitness, $O_{q}^{2}\left(\right.$ i.e. $\left.O_{\sigma^{\prime}}^{2}\right)$, and can then be considered as a fraction of the opportunity for selection on females, as well as its contribution to the total opportunity for selection, where $I_{0^{7}}=1 / R\left(I_{\varphi}\right)+I_{\text {mates }}($ see $[26,27]$ and $\S 2 c(i i))$.

## (c) Identifying the appropriate parameters for females

## (i) Fundamental parameters

As explained above, the proportions of successful and unsuccessfully breeding females, $p_{\mathrm{S} \rho}$, and $p_{0 \rho}$, the mean and variance in female offspring numbers, $O_{q}$ and $V_{\mathrm{O} Q}$, and the opportunity for selection on females, $I_{q}$, can all be easily estimated from molecular parentage data, provided that all parents and offspring in the population can be identified [1]. Also, as explained above, the quality of such data will determine the power of the inferences possible from such analyses. As with males, identification of the nonbreeding class of females can be exceptionally difficult, and while some data are better than none, the smaller the proportion of the population included in the sample, the weaker inferences about selection can be.

## (ii) The covariance between mating numbers and offspring numbers for females

The covariance between female mating number and the number of offspring produced by females equals
$\operatorname{Cov}_{\varrho}(m, o)=\left(\frac{\sum\left[m_{j} o_{j}\right]}{N_{\emptyset}}\right)-\left(O_{\varrho}\right)\left(P_{¢}\right)$,
where $m_{i} 0_{j}$ is the product of individual matings and offspring numbers for each $j$ th female, $N_{\text {Q }}$ is the total number of females, $O_{\varnothing}$ is the average number of offspring per female, and $P_{q}$ is the average female mating number promiscuity [1], i.e. the average number of matings per female, wherein each mating, whether with the same or with a different partner, is counted as a single event.

## (iii) Combining $\operatorname{Cov}_{q}(m, 0)$ with $\operatorname{Cov}_{O^{7}}(m, 0)$

As explained in Wade \& Shuster [101], whether $\operatorname{Cov}_{p}(m, 0)$ is positive, negative or zero determines whether females gain fitness, lose fitness or have no fitness consequences associated with multiple mating. However, additional information not explained in [101] may be obtained by considering whether females with these possible values for $\operatorname{Cov}_{q}(m, o)$ happen to mate with males who have corresponding or different values for $\mathrm{Cov}_{0^{\prime}}(m, o)$. Several 'zones' of combinations arise when $\operatorname{Cov}_{\rho}(m, o)$ and $\operatorname{Cov}_{O^{\prime}}(m, o)$ have positive, negative or zero values (figure $2 a, b$ ). The largest zone appears when either $\operatorname{Cov}_{\sigma^{( }}(m, o)$ and/or $\operatorname{Cov}_{q}(m, o)$ is zero (figure 2a). Fertilization success within this zone is randomly distributed across mating pairs, either because females use sperm at random or because male fertilization success is randomly distributed. This zone identifies WFS post-mating competition as described in $\S 2 c$ (iv) [1]. While post-mating sexual selection within this zone may behave like a lottery [8,10], lottery-like conditions are likely to occur only when $\operatorname{Cov}_{\rho}(m, o)$ is zero and $\operatorname{Cov}_{0^{\prime}}(m, o)$ is positive, because only in this cell are males likely to gain by producing large amounts of sperm.
(a)

| $\begin{aligned} & 0 \\ & \hat{5} \\ & \overbrace{0}^{\pi} \\ & 0 \end{aligned}$ |  | Q mate at random;万 mate seldom; $\widehat{\sigma}$ success random (WFS) |  |
| :---: | :---: | :---: | :---: |
|  | q mate seldom; <br> § success random (WFS) | $q$ mate at random; §success random (WFS) | q mate often; §'success random (WFS) |
|  |  | $q$ mate at random; <br> § mate often; đ success random or as lottery (WFS or WFA) |  |

(b) $\quad \operatorname{Cov}_{Q}(m, o)$

numbers are likely to be self-reinforcing. This zone identifies a scenario that could be called WFO; a mating system, which, as mentioned, describes situations now known as genetic complementarity [49,109,110].

When $\operatorname{Cov}_{\rho}(m, o)$ is positive and $\operatorname{Cov}_{0^{\prime}}(m, o)$ is negative, post-mating sexual selection is likely to be weak because females will seek multiple matings but males will not (figure $2 b$ ). Multiple mating by females could lead to multiple sires per clutch if sperm precedence is incomplete, or if males are unable to guard their mates. However, if males are successful at either endeavour, this zone identifies another cell in which 'WFA' [1], and if spermatic success in the latter case is accomplished by mate guarding, post-mating sexual selection cannot occur here. If sperm precedence is incomplete, $\operatorname{Cov}_{0^{\prime}}(m, o)$ may become zero. However, sexual selection in any case is likely to be reduced because males are unlikely to seek multiple matings ( $\operatorname{Cov}_{0^{2}}(m, o)$ is negative), and males successful at mate guarding will limit their mate numbers, increasing the number of males in the population able to sire young.

When both $\operatorname{Cov}_{q}(m, o)$ and $\operatorname{Cov}_{0^{( }}(m, o)$ are positive, males as well as females who engage in multiple matings gain high fitness (figure $2 b$ ). This combination could reinforce a genetic correlation between male and female tendencies to mate multiple times within mated pairs [137,138], and if repeatedly mating pairs experience the highest fitness, this mating system could represent 'runaway monogamy'. This zone too identifies a situation in which 'WFA', but again, postmating sexual selection by any mechanism is unlikely because males who mate repeatedly with only their partners do not obtain multiple mates.

If females tend not to cluster their mating with particular males, but instead change partners with each mating, postmating sexual selection could increase in this scenario, but only if, among the males who mate repeatedly with different partners, particular males fertilize most or all of their mates' ova. If this condition exists, sexual selection can intensify, but stronger sexual selection means that fitness variance among females becomes proportionally weaker [1]. This mating system could also represent 'non-lottery' sperm competition wherein particular sperm traits rather than large ejaculate volumes are favoured, but, although predicted in theory [6,7], whether such traits are widespread in nature is somewhat unclear. Genetic correlations between sperm traits and various traits in female reproductive tracts are known [132], but co-evolution of genetically correlated traits need not involve direct competition among males (e.g. via sperm competition) and are unlikely to directly benefit female fitness [1]. Modifications of sperm traits in response to ovum density are known to exist, but evidence in broadcast spawners suggests that these traits evolve in response to female adaptations to avoid polyspermy rather than in response to sperm competition [60]. Note: An opportunity to quantitatively distinguish sperm competition from cryptic female choice may exist in such systems. Longer, faster sperm appear to correlate with greater promiscuity in cichlid fish [68], but such data appear to be rare across taxa [60,68], and could also be a response to female adaptations to avoid polyspermy or sperm limitation when the egg density is high. If females mate promiscuously and sperm precedence is incomplete, or if males in this scenario become depleted of sperm, this system will change to one in which $\operatorname{Cov}_{0^{7}}(m, 0)$ is zero (WFS), where post-mating sexual selection is unlikely, or possibly one that is negative (WFO), wherein mate-guarding males


Figure 3. Possible relative values for the sex difference in the opportunity for selection (i.e. the opportunity for sexual selection), $I_{\text {mates, }}$ arising from multiple mating and post-mating sexual selection, based on the sign of the covariance in mating numbers and offspring numbers for each sex; grey bars indicate the likely values of $I_{\text {mates }}$ due to processes other than post-mating sexual selection; black bars indicate where post-mating sexual selection is likely, i.e. where $\operatorname{Cov}_{0^{\prime}}(m, 0)$ is positive, $\operatorname{Cov}_{o}(m, 0)$ is zero, and if certain males are capable of producing abundant sperm; hatched bars indicate where post-mating sexual selection is possible, where both $\operatorname{Cov}_{0^{7}}(m, 0)$ and $\operatorname{Cov}_{\rho}(m, 0)$ are positive, females change partners with each mating and if 'non-lottery' sperm competition occurs.
ensure their paternity. In either case, neither sperm competition nor cryptic female choice are likely to be sources of sexual selection (figure $2 b$ ).

When $\operatorname{Cov}_{0^{\prime}}(m, o)$ is positive and $\operatorname{Cov}_{q}(m, o)$ is negative, males gain by multiple mating but females do not (figure $2 b$ ). Here, sexual selection could become extremely strong because males will attempt to mate with multiple females and females will tend to avoid multiple mating. This zone identifies what has been called 'chase-away' sexual selection [48] (but also see [1]) and it too identifies 'WFA'. However, in this case too, females tend to mate rarely and, therefore, post-mating sexual selection is unlikely to occur despite the fact that sexual selection itself is likely to be more powerful than any of the above scenarios; here, males may be highly variable in their mate numbers but females are not.

Figure 3 summarizes possible relative values of the opportunity for sexual selection, $I_{\text {mates }}$, based on the above discussion of different combinations of the covariance between mating numbers and offspring numbers for each sex, $\operatorname{Cov}_{0^{f}}(m, 0)$ and $\operatorname{Cov}_{p}(m, 0)$. In general, this diagram reveals $2 / 9$ scenarios in which post-mating sexual selection is possible, but even in these cases only under particular circumstances: (i) where $\operatorname{Cov}_{0^{\prime}}(m, o)$ is positive, $\operatorname{Cov}_{q}(m, o)$ is zero, and certain males are capable of producing abundant sperm, and (ii) where both $\operatorname{Cov}_{0^{\prime}}(m, 0)$ and $\operatorname{Cov}_{\rho}(m, 0)$ are positive, females change partners with each mating, and 'non-lottery' sperm competition is possible. Note that the opportunity for post-mating sexual selection in each of these scenarios is expected to be less intense than when $\operatorname{Cov}_{\sigma^{\prime}}(m, 0)$ is positive and $\operatorname{Cov}_{q}(m, 0)$ is negative, a situation in which sexual selection is likely to be strong, but post-mating sexual selection is unlikely to occur.
(iv) The variance in fitness caused by female life-history traits The above circumstances describe how mating behaviour by females enhances or diminishes the strength of sexual
selection, but females may influence sexual selection in other ways as well, through variation in (i) the number of times they mate and (ii) the number of reproductive events in a female's lifetime, which may depend on the duration of female reproductive competency [1]. Accordingly, females who mate once in their lifetime are monandrous, whereas females who mate more than once are polyandrous (the term 'polyandry' is frequently used to describe the latter condition, but we subscribe to the genetic, rather than the social definition of the mating system [1], wherein polyandry describes a genetic mating system in which females are variable in mate numbers, but males are not, with males having no more than one mate within their lifetime). Females who produce a single clutch of offspring are semelparous, whereas females who produce multiple clutches of offspring are iteroparous. Among iteroparous females, the longer the duration of female reproductive competency, the more variation in the pattern of female reproduction within and among seasons is possible, and simultaneously, the more variable the identities of males serving as mates for such females can be.

Wade [100] considered multiple mating and iteroparity by females similar in their effects on the opportunity for selection to the effects of multiple mating by males. He identified the term $I_{\text {clutches }}$ to describe the variance in clutch number among females, $V_{\text {clutches, }}$ divided by the squared average number of clutches per female, $\mathrm{C}^{2}$, noting that when females mate more than once, they divide each clutch into sub-clutches, equal in number to the number of sires. Wade [100] argued that multiple mating and iteroparity among females interchangeably decrease the variance in fitness among males and so increase the variance in fitness among females such that $I_{O^{7}}-I_{Q}=I_{\text {mates }}-I_{\text {clutches. }}$. As explained above, the production of multiple clutches either by multiple mating or by iteroparity increases the variance in female fitness, and it allows more males to mate. Both tendencies decrease the variance in fitness among males and so decrease the opportunity for sexual selection [1].

Shuster \& Wade [1] showed that when females mate more than once and produce multiple clutches of offspring, the total variance in offspring numbers for females, $V_{\mathrm{O} \text { o }}$, is influenced by three distinct effects arising from variation in female clutch size (cs): (i) the variance in offspring numbers averaged across all females, $V_{\mathrm{cs}, \text { clutch, }}$ a value expected to become larger as females produce multiple clutches; (ii) the variance in offspring numbers due to the effects of mating with different sires on clutch size, $V_{\text {cs,sires, }}$ a value expected to become larger as females mate more than once; and (iii) the variance in offspring numbers due to differences in the average clutch size that females produce, $V_{\mathrm{cs}, \text { females }}$. The first two components of variance in female fitness are equivalent to the variance in offspring numbers within females, thus, $V_{\mathrm{O} \text { q within }}=V_{\mathrm{cs}, \mathrm{clutch}}+V_{\mathrm{cs}, \text { sires }}$. The third female fitness component is equivalent to the variance in offspring number among females, or $V_{\mathrm{O} \text { among }}=V_{\mathrm{cs}, \text { females }}$.

As in the study of Wade [100], this approach provides a means for identifying the relative influences of multiple sires and multiple clutches on the total variance in offspring numbers for females. However, unlike Wade [100], this approach focuses not on how the number of clutches or sub-clutches females have may influence $V_{\mathrm{O} \text { ¢ }}$, but rather on how individual female fitness may become variable due to the effects of multiple males and multiple reproductive
events. This approach [1] identifies $V_{\text {Oqwithin }}$ as the component of variance in offspring numbers affected by different numbers of sires and clutches, because the effect of multiple mating and multiple clutch numbers on the total variance in female offspring numbers arises from within individual females. Thus, to explore these effects, individual females must have life histories that include matings with multiple mates and the production of multiple clutches, or researchers must create these circumstances experimentally. When divided by the squared average in female offspring numbers, $O_{9}^{2}$, the relationship explained above becomes, $I_{Q}=\left(I_{\mathrm{cs}, \text { clutch }}+I_{\mathrm{cs}, \text { sires }}\right)+I_{\mathrm{cs}, \text { females }}$.

To explore the effects of multiple mating on the amongfemale component of variance in female offspring numbers, females must be divided into $k$ classes that identify the number of mates (or matings) females experience for each clutch of offspring they produce. The total variance in female fitness, in terms of offspring numbers, $V_{\text {Optotal }}$, can once again be partitioned into two components, but this time $V_{\mathrm{O} \text { within }}$ is the average of the variances in offspring number within the classes of females who mate with different numbers of males, and $V_{\mathrm{O} \text { ofamong }}$ is the variance in the average number of offspring among the mating and non-mating female classes, where $V_{\mathrm{O} \text { Ototal }}=V_{\mathrm{O} \text { 早within }}+V_{\mathrm{O} \text { among, }}$ or, by substitution,

where $k$ represents each class of females based on their number of mates, $p_{\mathrm{k}}$ represents the proportion of females belonging to each $k$ th class, $K$ equals the average number of mates or matings per female (i.e. $N_{O^{7}} / N_{Q}=1 / R$ ), $c$ equals the average number of clutches per female, and $k\left(O_{q}\right)$ and $k\left(V_{\mathrm{O} q}\right)$ represent the mean and variance in offspring numbers, respectively, for females within each $k$ th mate or mating class, and where $O_{q}$ and $V_{\mathrm{O}}^{\mathrm{O}} \mathrm{e}$ equal the mean and variance in offspring numbers per female. Collecting terms and assuming $R=1$, we have
$V_{\mathrm{O} \text { ¢total }}=K\left(V_{\mathrm{O}}^{\mathrm{O}}\right)+O_{\varrho}^{2} V_{\text {Omating number }}$,
which, when divided by the squared average in female fitness, $\left(K O_{\text {}}\right)^{2}$, equation (3.3) becomes
$I_{\varphi \text { total }}=I_{\varphi \text { cs }}+I_{\varphi \text { mating number }}$.
Each of the three approaches above captures a different aspect of the effects of multiple mating on females. The first approach (cf. [100]) identifies the effects of variation in clutch size and clutch number on total variance in female offspring numbers. The second approach (cf. [1]) identifies the effects that multiple mates and multiple reproductive events may have on the variance in clutch sizes within individual females. The third approach identifies the effects that variation in mating number, either with the same or with different males, has on the total variance in female offspring numbers. Which approach is used depends on the experimental question asked. As explained above, the relative contribution of each of the variance components can be compared by dividing each by the squared average in female fitness, as well as compared in ratio form to $I_{\varphi}$, which can be examined relative to $I_{O^{か}}$ and $\Delta I$ [1].
(d) Measuring the appropriate parameters for females As explained above for males, while each of these parameters can be calculated explicitly if the numbers of successful and unsuccessful individuals in the population are known, these
data can be extremely difficult to collect and so often go unrecorded. Table 3 summarizes the extent to which the above parameters have been investigated in studies to date. Abundant information appears to exist on the sources of variance in female offspring numbers, as well as on the apparent values for $\operatorname{Cov}_{p}(m, o)$, although in most cases values can only be inferred from experimental results rather than actual data. In contrast, the proportion of unsuccessful females, $p_{00}$, and the opportunity for selection on females, $I_{\varphi}$, are seldom quantified.

We emphasize again that such information is crucial to actual measurements of the opportunity for selection on females as well as the covariance between mating numbers and offspring number for both sexes. To show that either males or females benefit by multiple mating, it is necessary to show that a covariance between mate numbers and offspring numbers exists. Yet without examining the magnitude of these values, as explained above, it is impossible to conclude that post-mating sexual selection is strong or weak. Moreover, without measuring these values for females and comparing them to the magnitude of values collected for males, it is impossible to say whether females gain significant fitness from multiple mating relative to the total opportunity for selection.

## 4. Discussion

We present four major results. First, we suggest that when post-mating sexual selection is strong, i.e. when particular males gain from multiple mating, the fitness advantages females gain from males through multiple mating are likely to be proportionately weak. This relationship exists because when fewer males secure mates, the among-group component of the male variance in relative fitness becomes extremely large (figure 1), and so becomes a proportionately larger fraction of total selection $[1,26,27,100]$. Because the opportunity for sexual selection equals the sex difference in the opportunity for selection, $\Delta I=I_{0^{7}}-I_{\odot}$ [1], when sexual selection is strong, $I_{\rho}$ must be proportionately small. Conversely, when females engage in mating with multiple males and produce multiple clutches, the increased variance in female fitness is likely to erode the intensity of sexual selection most severely. Thus, when female fitness variance is proportionately large, the sex difference in the opportunity for selection must be proportionately small. This relationship has recently been documented experimentally in junglefowl, Gallus gallus [86] (see also [136]), and is expected to exist regardless of how sexual selection occurs [1].

Second, we provide a method for estimating the variance in fitness and the opportunity for selection resulting from postmating sexual selection. Several researchers have recently used ANOVA to partition out this effect as part of their experimental design [3,4,31,86]. Our method complements this approach but has the advantage of not requiring that offspring be assigned to parents in a probabilistic way; our method explicitly assigns offspring to each parent. Our approach is also useful for examining existing datasets for which the proportions of individuals who mate and successfully produce offspring, who mate and fail to produce offspring, and who fail to mate at all, are known [3,4]. As we show, our approach is useful for gonochoristic as well as hermaphroditic species.

Our third major result is our finding that post-mating sexual selection occurs in only two of the nine possible mating systems in which multiple mating by females can
occur: (i) when females have multiple mates and males are able to produce large volumes of sperm; and (ii) when females have multiple males and males have particular adaptations that allow their sperm to be competitive. There are other situations in which females may mate with multiple males, but because $\operatorname{Cov}(m, o)$ is zero or negative in these scenarios for one or both sexes, post-mating sexual selection is either unlikely or impossible. We acknowledge that the circumstances we identify in which post-mating sexual selection is likely to occur, are those in which most of the current evidence for sperm competition already exists, a condition that seems to be frequently observed in insects. However, the current literature on sperm competition, in our view, implies that such conditions are ubiquitous and strong in a large number of taxa. We argue that they may not be. Therefore, it is our goal to show that, while possibly unusually common in insects, this particular scenario actually represents a fraction of the possible conditions in which post-mating sexual selection could occur, and a highly contingent set of circumstances at that. We assert that if you look for sperm competition under such circumstances, you are likely to find it. We also assert, and we think justifiably, that such conditions overall may be comparatively rare. We hope that future research considers these scenarios more closely so that research on post-mating sexual selection may become more focused as well.

A fourth major result of our analyses is that we have found few recorded studies in which the overall strength of post-mating sexual selection and the presumed benefits females gain by multiple mating have been considered together in terms of the sex difference in the opportunity for selection ( $[1,3,4]$; tables $1-3$ ). The approach allows the relative contributions of these two consequences of polyandrous mating to be considered simultaneously. This result places some doubt on the conclusions of many presumed examples of the evolution of male traits by sperm competition or evolution of female traits by multiple mating; not because these experiments are not carefully executed, but rather because the relative intensity of selection in these contexts, as well as the context of selection itself, is yet unknown.

We have proposed a framework for measuring postmating sexual selection, requiring highly specific information that is extremely difficult to obtain. In particular, we encourage researchers to document the classes of nonreproducing individuals in each sex because this allows the sex difference the opportunity for selection to be quantified, because it allows the specific effects of post-mating competition to be isolated and because it expands the focus of fitness measurement beyond the class of successfully reproducing individuals. We acknowledge that this procedure in some cases may confound sexual selection with other selective contexts. However, if one sex experiences greater fitness variance than the other for any reason, it will generate sex-specific selection, which, at least in gonochoristic species, is likely to lead to sexual dimorphism. In our view, such selection, even if operating in reproductive contexts not clearly identifiable as male combat or female choice, can be considered sexual selection [1,2]. We also advocate quantification of the covariance between mating number and offspring number for both sexes, $\operatorname{Cov}(m, 0)$, primarily because this parameter provides an estimate of the strength of selection favouring multiple mating in each sex in the form of Bateman gradients ([94,95], tables 1 and 3). However, an
additional unappreciated advantage of examining this covariance for both sexes simultaneously is that it provides a means for predicting mating systems in which post-mating sexual selection is possible and in which it is not.

We have proposed that estimates of sexual selection on males are incomplete without estimates of how multiple mating and multiple reproductive events by females may erode the strength of sexual selection [1]. We advocate three quantitative approaches for investigating the variance in fitness among females due to differences in female life-history that can be tailored to the experimental systems available. These approaches allow quantification of the effects of multiple matings, multiple sires and multiple reproductive events on the opportunity for selection on females. With this information, it becomes possible not only to scale the evolutionary effects of female reproductive life-history relative to sexual selection, but also to examine the magnitude of selection on multiple mating by females relative to total selection. We appear to be asking researchers to conform only to our specific criteria; but that is
neither our intent nor what our suggestions amount to in practice. Our suggestions as well as those of others who emphasize a quantitative approach conform to standard evolutionary genetic theory and results. Our goal is to encourage current research to align itself with the principles it claims to promote. We argue that to understand the process of sexual selection, in this or any context, it is necessary to consider the role each sex plays in the process. Without such conjoined information, it is likely that the resulting incomplete answers will be misguided or wrong. In summary, our results suggest that existing theory and data on post-mating sexual selection are incomplete. We hope our analysis will be greeted, not with disdain, but rather with enthusiasm for investigating when post-mating sexual selection occurs, when it does not, and why.

We are grateful to Michael J. Wade for his fundamental contributions to the ideas discussed above as well as for his comments on an earlier draft of this manuscript. We are also grateful to Tommaso Pizzari and two anonymous reviewers, whose comments and suggestions greatly improved this manuscript.

## References

1. Shuster S, Wade M. 2003 Mating systems and strategies. Princeton, NJ: Princeton University Press.
2. Darwin CR. 1874. The descent of man and selection in relation to sex, 2nd edn. New York, NY: Rand, McNally and Co.
3. Anthes N et al. 2010 Bateman gradients in hermaphrodites: an extended approach to quantify sexual selection. Am. Nat. 173, 249-263. (doi:10. 1086/655218)
4. Pélissié B, Jarne P, David P. 2012 Sexual selection without sexual dimorphism: Bateman gradients in a simultaneous hermaphrodite. Evolution 66, 66-81. (doi:10.1111/j.1558-5646. 2011.01442.x)
5. Webster M, Pruett-Jones S, Westneat D, Arnold SJ. 1995 Measuring the effects of pairing success, extra-pair copulations and mate quality on the opportunity for sexual selection. Evolution 49, 1147-1157. (doi:10.2307/2410439)
6. Pitnick S, Hosken DJ, Birkhead TR. 2009 Sperm morphological diversity. In Sperm biology: an evolutionary perspective. (eds TR Birkhead, DJ Hosken, S Pitnick), pp. 69-149. Burlington, MA: Academic Press.
7. Pizzari T, Parker GA. 2009 Sperm competition and the sperm phenotype. In Sperm biology: an evolutionary perspective (eds TR Birkhead, DJ Hosken, S Pitnick), pp. 207-245. Burlington, MA: Academic Press.
8. Parker GA, Plzzari T. 2010 Sperm competition and ejaculate economics. Biol. Rev. 85, 897-934. (doi:10.1111/j.1469-185X.2010.00140.x)
9. Smith RL. 1984 Sperm competition and the evolution of animal mating systems. San Diego, CA: Academic Press.
10. Birkhead T, Møller AP. 1998 Sperm competition and sexual selection. San Diego, CA: Academic Press.
11. Levine L. 1967 Sexual selection in mice. IV Experimental demonstration of selective
fertilization. Am. Nat. 101, 289-294. (doi:10.1086/ 282491)
12. Hotzy C, Arnquist G. 2009 Sperm competition favors harmful males in seed beetles. Curr. Biol. 19, 404-407. (doi:10.1016/j.cub.2009.01.045)
13. Cheng KM, Siegel PB. 1990 Quantitative genetics of multiple mating. Anim. Behav. 40, 406-407.
(doi:10.1016/S0003-3472(05)80939-X)
14. Birkhead T. 1999 Reproductive biology: distinguished sperm in competition. Nature 400, 406-407. (doi:10.1038/22650)
15. Gage MJG, Macfarlane CP, Yeates S, Ward RG, Searle JB, Parker GA. 2004 Spermatozoal traits and sperm competition in Atlantic salmon: relative sperm velocity is the primary determinant of fertilization success. Curr. Biol. 14, 44-47. (doi:10.1016/j.cub. 2003.12.028)
16. García-González F, Simmons LW. 2005 The evolution of polyandry: intrinsic sire effects contribute to embryo viability. J. Evol. Biol. 18, 1097-1103. (doi:10.1111/j.1420-9101.2005.00889.x)
17. Vladić TV, Järvi T. 2001 Sperm quality in the alternative reproductive tactics of Atlantic salmon: the importance of the loaded raffle mechanism. Proc. R. Soc. Lond. B 268, 2375-2381. (doi:10. 1098/rspb.2001.1768)
18. Short RV. 1979 Sex determination and differentiation. Brit. Med. Bull. 35, 121-127.
19. Hosken D, Ward P. 2001 Experimental evidence for testis size evolution via sperm competition. Ecol. Lett. 4, 10-13. (doi:10.1046/j.1461-0248.2001. 00198.x)
20. Wedell N, Gage MJG, Parker GA. 2002 Sperm competition, male prudence and sperm-limited females. Trends Ecol. Evol. 17, 313-320. (doi:10.1016/S0169-5347(02)02533-8)
21. Gage MJG, Freckleton RP. 2003 Relative testis size and sperm morphometry across mammals: no evidence for an association between sperm
competition and sperm length. Proc. R. Soc. Lond. B 270, 625-632. (doi:10.1098/rspb. 2002.2258)
22. Pizzari T, Birkhead TR. 2000 Female feral fowl eject sperm of subdominant males. Nature 405, 787-789. (doi:10.1038/35015558)
23. Foster K, Seppä P, Ratnieks FLW, Thorén PA. 1999 Low paternity in the hornet Vespa crabro indicates that multiple mating by queens is derived in vespine wasps. Behav. Ecol. Sociobiol. 46, 252-257. (doi:10.1007/s002650050617)
24. Bartmann S, Gerlach G. 2001 Multiple paternity and similar variance in reproductive success of male and female wood mice (Apodemus sylvaticus) housed in an enclosure. Ethology 107, 889-899. (doi:10. 1046/j.1439-0310.2001.00723.x)
25. Dean MD, Ardlie KG, Nachman MW. 2006 The frequency of multiple paternity suggests that sperm competition is common in house mice (Mus domesticus). Mol. Ecol. 15, 4141-4151. (doi:10. 1111/j.1365-294X.2006.03068.x)
26. Wade MJ. 1979 Sexual selection and variance in reproductive success. Am.Nat. 114, 742-747. (doi:10.1086/283520)
27. Wade MJ, Arnold SJ. 1980 The intensity of sexual selection in relation to male sexual behaviour, female choice, and sperm precedence. Anim. Behav. 28, 446-461. (doi:10.1016/S0003-3472 (80)80052-2)
28. Bjork A, Pitnick S. 2006 Intensity of sexual selection along the road to isogamy. Nature 441, 742-745 (doi:10.1038/nature04683)
29. Portnoy DS, Piercy AN, Musick JA, Burgess GH, Graves JE. 2007 Genetic polyandry and sexual conflict in the sandbar shark, Carcharhinus plumbeus, in the western North Atlantic and Gulf of Mexico. Mol. Ecol. 16, 187-197. (doi:10.1111/j. 1365-294X.2006.03138.x)
30. Møller AP, Ninni P. 1998 Review. Sperm competition and sexual selection: a meta-analysis of paternity
studies of birds. Behav. Ecol. Sociobiol. 43,
345-358. (doi:10.1007/s002650050501)
31. Pischedda A, Rice WR. 2012 Partitioning sexual selection into its mating success and fertilization success components. Proc. Natl Acad. Sci. USA 109, 2049-2053. (doi:10.1073/pnas.1110841109)
32. Marshall DJ, Evans JP. 2005 The benefits of polyandry in the free-spawning polychaete Galeolaria caespitosa. J. Evol. Biol. 18, 735-741. (doi:10.1111/j.1420-9101.2004.00873.x)
33. Simmons LW, Kvarnemo C. 1997 Ejaculate expenditure by male bushcrickets decreases with sperm competition intensity. Proc. R. Soc. Lond. B
264, 1203-1208. (doi:10.1098/sppb.1997.0166)
34. Simmons LW, Craig M, Llorens T, Schinzig M, Hosken D. 1993 Bushcricket spermatophores vary in accord with sperm competition and parental investment theory. Proc. R. Soc. Lond. B 251, 183-186. (doi:10.1098/sppb.1993.0027)
35. Backus V, Cade WH. 1986 Sperm competition in the field cricket Gryllus integer (Orthoptera: Gryllidae). Fla. Entomol. 69, 722-728. (doi:10. 2307/3495220)
36. Fedorka K, Mousseau TA. 2002 Material and genetic benefits of female multiple mating and polyandry. Anim. Behav. 64, 361-367. (doi:10.1006/anbe. 2002.3052)
37. Bretman A, Newcombe D, Tregenza T. 2009 Promiscuous females avoid inbreeding by controlling sperm storage. Mol. Ecol. 18, 33403345. (doi:10.1111/j.1365-294X.2009.04301.x)
38. Pol RG, Casenave JL, Feldhaar H, Milesi FA, Gadau J. 2008 Polyandry in two South American harvester ants. Insect. Soc. 55, 91-97. (doi:10.1007/s00040-007-0975-0)
39. Kellner K, Trindl A, Heinze J, D'Ettorre P. 2007 Polygyny and polyandry in small ant societies. Mol. Ecol. 16, 2363-2369. (doi:10.1111/j.1365-294X. 2007.03297x)
40. Sakurai G, Kasuya E. 2008 Different female mating rates in different populations do not reflect the benefits the females gain from polyandry in the adzuki bean beetle. J. Ethol. 26, 93-98. (doi:10. 1007/s10164-007-0036-1)
41. Tregenza T, Attia F, Bushaiba SS. 2009 Repeatability and heritability of sperm competition outcomes in males and females of Tribolium castaneum. Behav. Ecol. Sociobiol. 63, 817-823. (doi:10.1007/s00265-009-0716-7)
42. Lewis SM, Austad SN. 1990 Sources of intraspecific variation in sperm precedence in red flour beetles. Am. Nat. 135, 351-359. (doi:10.1086/285050)
43. Moya-Larano J, Fox CW. 2006 Ejaculate size, second male size, and moderate polyandry increase female fecundity in a seed beetle. Behav. Ecol. 17, 940 946. (doi:10.1093/beheco/arl029)
44. Demary KC, Lewis SM. 2007 Male reproductive allocation in fireflies (Photinus spp.). Invertebr. Biol. 126, 74-80. (doi:10.1111/j.1744-7410.2007. 00078.x)
45. Cook PA, Gage MJG. 1995 Effects of risks of sperm on the numbers competition of eupyrene and apyrene sperm ejaculated by the moth Plodia
interpunctella (Lepidoptera: Pyralidae). Behav. Ecol. Sociobiol. 36, 261-268. (doi:10.1007/BF00165835)
46. Dunn DW, Sumner JP, Goulson D. 2005 The benefits of multiple mating to female seaweed flies, Coelopa frigida (Diptera: Coelpidae). Behav. Ecol. Sociobiol. 58, 128-135. (doi:10.1007/500265-005-0922-x)
47. Frentiu FD, Chenoweth SF. 2008 Polyandry and paternity skew in natural and experimental populations of Drosophila serrata. Mol. Ecol. 17, 1589-96. (doi:10.1111/j.1365-294x.2008.03693.x)
48. Holland B, Rice WR. 1999 Experimental removal of sexual selection reverses intersexual antagonistic coevolution and removes a reproductive load. Proc. Natl Acad. Sci. USA 96, 5083-5088. (doi:10.1073/ pnas.96.9.5083)
49. Clark AG, Begun DJ, Prout T. 1999 Female $\times$ male interactions in drosophila sperm competition.
Science 283, 217-220. (doi:10.1126/science.283. 5399.217)
50. Pitnick S, Brown WD, Miller GT. 2001 Evolution of female remating behaviour following experimental removal of sexual selection. Proc. R. Soc. Lond. B 268, 557-563. (doi:10.1098/sppb.2000.1400)
51. Bateman AJ. 1948 Intra-sexual selection in Drosophila. Heredity 2, 349-368. (doi:10.1038/hdy. 1948.21)
52. Gosselin T, Sainte-Marie B, Bernatchez L. 2005 Geographic variation of multiple paternity in the American lobster, Homarus americanus. Mol. Ecol. 14, 1517-1525. (doi:10.1111/j.1365-294X.2005. 02498.x)
53. Jivoff P. 1997 The relative roles of predation and sperm competition on the duration of the postcopulatory association between the sexes in the blue crab, Callinectes sapidus. Behav. Ecol. Sociobiol. 40, 175-185. (doi:10.1007/5002650050331)
54. Todd CD, Stevenson RJ, Reinardy H, Ritchie MG. 2005 Polyandry in the ectoparasitic copepod Lepeophtheirus salmonis despite complex precopulatory and postcopulatory mate-guarding. Mar. Ecol. Prog. Ser. 303, 225-234. (doi:10.3354/ meps303225)
55. Elgar MA, Bruce MJ, Crespigny FECD, Cutler AR, Cutler CL, Gaskett AC, Herberstein ME, Ramamurthy S, Schneider JM. 2003 Male mate choice and patterns of paternity in the polyandrous, sexually cannibalistic orb-web spider, Nephila plumipes. Aust. J. Zool. 51, 357-365. (doi:10.1071/Z002079)
56. Zeh JA, Newcomer SD, Zeh DW. 1998 Polyandrous females discriminate against previous mates. Proc. Natl Acad. Sci. USA 95, 13732-13736. (doi:10. 1073/pnas.95.23.13732)
57. Harper FM, Hart MW. 2005 Gamete compatibility and sperm competition affect paternity and hybridization between sympatric Asterias sea stars. Biol. Bull. 209, 113-126. (doi:10.2307/3593129)
58. Evans JP, Marshall DJ. 2005 Male-by-female interactions influence fertilization success and mediate the benefits of polyandry in the sea urchin Heliocidaris erythrogramma. Evolution 59, 106-112. (doi:10.1111/j.0014-3820.2005.tb00898.x)
59. Marshall DJ, Evans JP. 2007 Context-dependent genetic benefits of polyandry in a marine
hermaphrodite. Biol. Lett. 3, 685-688. (doi:10. 1098/rsbl.2007.0438)
60. Crean AJ, Marshall DJ. 2008 Gamete plasticity in a broadcast spawning marine invertebrate. Proc. Natl Acad. Sci. USA 105, 13 508-13513. (doi:10.1073/ pnas.0806590105)
61. Gage MJG, Stockley P, Parker GA. 1995 Effects of alternative male mating strategies on characteristics of sperm production in the Atlantic salmon (Salmo salar): theoretical and empirical investigations.
Proc. R. Soc. Lond. B 350, 391-399. (doi:10.1098/ rstb.1995.0173)
62. Immler S, Taborsky M. 2009 Sequential polyandry affords post-mating sexual selection in the mouths of cichlid females. Behav. Ecol. Sociobiol. 63, 1219-1230. (doi:10.1007/s00265-009-0744-3)
63. Bechert SA, Magurran AE. 2004 Multiple mating and reproductive skew in Trinidadian guppies. Proc. R. Soc. Lond. B 271, 1009-1014. (doi:10.1098/sppb.2004.2701)
64. King JR, Withler RE. 2005 Male nest site fidelity and female serial polyandry in lingcod (Ophiodon elongatus, Hexagrammidae). Mol. Ecol. 14, 653-660. (doi:10.1111/j.1365-294x.2005.02438.x)
65. DiBattista JD, Feldheim KA, Gruber SH, Hendry AP. 2008 Are indirect genetic benefits associated with polyandry? Testing predictions in a natural population of lemon sharks. Mol. Ecol. 17, 783-95. (doi:10.1111/j.1365-294X.2007.03623.x)
66. Fuller RC. 1998 Sperm competition affects male behaviour and sperm output in the rainbow darter. Proc. R. Soc. Lond. B 265, 2365-2371. (doi:10. 1098/sppb.1998.0585)
67. Spence R, Smith C. 2006 Mating preference of female zebrafish, Danio rerio, in relation to male dominance. Behav. Ecol. 17, 779-783. (doi:10.1093/beheco/arl016)
68. Fitzzatrick JL, Montgomerie R, Desjardins JK, Stiver KA, Kolm N, Balshine S. 2009 Female promiscuity promotes the evolution of faster sperm in cichlid fishes. Proc. Natl Acad. Sci. USA 106, 1128-1132. (doi:10.1073/pnas.0809990106)
69. Roberts J, Standish R, Byrne P, Doughty P. 1999 Synchronous polyandry and multiple paternity in the frog Crinia georgiana (Anura: Myobatrachidae). Anim. Behav. 57, 721-726. (doi:10.1006/anbe.1998.1019)
70. Sztatecsny M, Jehle R, Burke T, Hödl W. 2006 Female polyandry under male harassment: the case of the common toad (Bufo bufo). J. Zool. 270, 517-522. (doi:10.1111/j.1469-7998.2006.00120.x)
71. Stille B, Madsen T, Niklasson M, Nikiasson M. 1986 Multiple paternity in the adder, Vipera berus. Oikos 47, 173-175. (doi:10.2307/3566042)
72. Fantin C, Viana LS, Monjeló LADS, Farias IP. 2008 Polyandry in Podocnemis unifilis (Pleurodira; Podocnemididae), the vulnerable yellow-spotted Amazon River turtle. Amphibia-Reptilia 29, 479-486. (doi:10.1163/156853808786230361)
73. Eizaguirre C, Laloi D, Massot $M$, Richard $M$, Federici P, Clobert J. 2007 Condition dependence of reproductive strategy and the benefits of polyandry in a viviparous lizard. Proc. R. SoC. B 274, 425-430. (doi:10.1098/sppb.2006.3740)
74. Lee PLM, Hays GC. 2004 Polyandry in a marine turtle: females make the best of a bad job. Proc. Natl Acad. Sci. USA 101, 6530-6535. (doi:10.1073/ pnas.0307982101)
75. Kissner KJ, Weatherhead PJ, Gibbs HL. 2005 Experimental assessment of ecological and phenotypic factors affecting male mating success and polyandry in northern watersnakes, Nerodia sipedon. Behav. Ecol. Sociobiol. 59, 207-214. (doi:10.1007/s00265-005-0026-7)
76. Moore JA, Nelson NJ, Keall SN, Daugherty CH. 2008 Implications of social dominance and multiple paternity for the genetic diversity of a captive-bred reptile population (tuatara). Conserv. Genet. 9, 1243-1251. (doi:10.1007/s10592-007-9452-6)
77. Prosser MR, Weatherhead PJ, Gibbs HL, Brown GP. 2002 Genetic analysis of the mating system and opportunity for sexual selection in northern water snakes (Nerodia sipedon). Behav. Ecol. 13, 800-807. (doi:10.1093/beheco/13.6.800)
78. Dietrich V, Schmoll T, Winkel W, Epplen J, Lubjuhn T. 2004 Pair identity: an important factor concerning variation in extra-pair paternity in the coal tit (Parus ater). Behaviour 141, 817-835. (doi:10. 1163/1568539042265644)
79. Burke T, Davies NB, Bruford MW, Hatchwell BJ. 1989 Parental care and mating related to paternity by DNA fingerprinting related to paternity by DNA fingerprinting. Nature 338, 249-251. (doi:10.1038/ 338249a0)
80. Faaborg J, Parker PG, DeLay L, de Vries T, Bednarz JC, Paz SM, Naranjo J, Waite TA. 1995 Confirmation of cooperative polyandry in the Galapagos hawk (Buteo galapagoensis). Behav. Ecol. Sociobiol. 36, 83-90. (doi:10.1007/BF00170712)
81. Heinsohn R, Ebert D, Legge S, Peakall R. 2007 Genetic evidence for cooperative polyandry in reverse dichromatic Eclectus parrots. Anim. Behav. 74, 10471054. (doi:10.1016/j.anbehav.2007.01.026)
82. Kleven 0, Fossøy F, Laskemoen T, Robertson RJ, Rudolfsen G, Lifjeld JT. 2009 Comparative evidence for the evolution of sperm swimming speed by sperm competition and female sperm storage duration in passerine birds. Evolution 63, 2466-2473. (doi:10. 1111/j.1558-5646.2009.00725.x)
83. Whittingham LA, Dunn PO, Magrath RD. 1997 Relatedness, polyandry and extra-group paternity in the cooperatively-breeding white-browed scrubwren (Sericornis frontalis). Behav. Ecol. Sociobiol. 40, 261-270. (doi:10.1007/s002650050341)
84. Piper WH, Slater G. 1993 Polyandry and incest avoidance in the cooperative stripe-backed wren of Venezuela. Behaviour 3, 227-247. (doi:10.1163/ 156853993X00597)
85. Dunn PO, Robertson RJ, Michaud-Freeman D, Boag PT. 1994 Extra-pair paternity in tree swallows: why do females mate with more than one male? Behav.Ecol. Sociobiol. 35, 273-281. (doi:10.1007/ BF00170708)
86. Collet J, Richardson DS, Worley K, Pizzari T. 2012 Sexual selection and the differential effect of polyandry. Proc. Natl Acad. Sci. USA 109, 8641-8645. (doi:10.1073/pnas.1200219109)
87. Carmichael LE, Szor G, Berteaux D, Giroux MA, Cameron C, Strobeck C. 2007 Free love in the far north: plural breeding and polyandry of arctic foxes (Alopex lagopus) on Bylot Island, Nunavut. Can. J. Zool. 85, 338-343. (doi:10.1139/Z07-014)
88. Fisher DO, Double MC, Blomberg SP, Jennions MD, Cockburn A. 2006 Post-mating sexual selection increases lifetime fitness of polyandrous females in the wild. Nature 444, 89-92. (doi:10.1038/ nature05206)
89. Kraaijeveld-Smit F, Ward S, Smith PT. 2002 Multiple paternity in a field population of a small carnivorous marsupial, the agile antechinus, Antechinus agilis. Behav. Ecol. Sociobiol. 52, 84-91. (doi:10.1007/ s00265-002-0485-z)
90. Keane B, Waser PM, Creel S, Creel NM, Elliott JF, Minchella DJ. 1994 Subordinate reproduction in dwarf mongooses. Anim. Behav. 47, 65-75. (doi:10.1006/anbe.1994.1008)
91. Baker A, Dietz JM, Kleiman DG. 1993 Behavioral evidence for monopolization of paternity in multimale groups of golden lion tamarins. Anim. Behav. 46, 1091-1103. (doi:10.1006/anbe.1993.1299)
92. Baker RJ, Makova KD, Chesser RK. 1999 Microsatellites indicate a high frequency of multiple paternity in Apodemus (Rodentia). Mol. Ecol. 8, 107-111. (doi:10.1046/j.1365-294X.1999.00541.x)
93. Booth W, Montgomery WI, Prodöhl PA. 2007 Polyandry by wood mice in natural populations. J. Zool. 273, 176-182. (doi:10.1111/j.1469-7998. 2007.00312.x)
94. Arnold SJ. 1994 Bateman's principles and the measurement of sexual selection in plants and animals. Am. Nat. 144, S126-S149. (doi:10.1086/ 285656)
95. Arnold SJ, Duvall D. 1994 Animal mating systems: a synthesis based on selection theory. Am. Nat.
143, 317 - 348. (doi:10.1086/285606)
96. Shuster S. 2009 Sexual selection and mating systems. Proc. Natl Acad. Sci. USA 106, 10009-10 016.
97. Parker G. 1970 Sperm competition and its evolutionary consequences in the insects. Biol. Rev. Cambr. Philos. Soc. 45, 525-567. (doi:10.1111/j. 1469-185X.1970.tb01176.x)
98. Lewis S, Austad S. 1994 Sexual selection in flour beetles: the relationship between sperm precedence and male olfactory attractiveness. Behav. Ecol. 5, 223-224. (doi:10.1093/beheco/5.2.223)
99. Clark AG, Aguade M, Prout T, Harshmad LG, Langley CH. 1995 Variation in sperm displacement and its association with accessory gland protein loci in Drosophila melanogaster. Genetics 139, 189-201. (doi:10.1073/pnas.0901132106)
100. Wade M. 1987 Measuring sexual selection. In Sexual selection: testing the alternatives (eds JW Bradbury, MB Andersson), pp. 197-207. New York, NY: John Wiley and Sons.
101. Wade MJ, Shuster SM. 2005 Don't throw Bateman out with the bathwater! Integr. Comp. Biol. 45, 945-51. (doi:10.1093/icb/45.5.945)
102. Crow JF. 1958 Some possibilities for measuring selection intensities in man. Hum. Biol. 30, 1-13.
103. Jones AG. 2009 On the opportunity for sexual selection, the Bateman gradient and the maximum intensity of sexual selection. Evolution 63, 1673-1684. (doi:10.1111/j.1558-5646.2009.00664.x)
104. Wade MJ, Shuster SM. 2004 Sexual selection: harem size and the variance in male reproductive success. Am. Nat. 164, E83-E89. (doi:10.1086/424531)
105. Shuster SM. 2010 Alternative mating strategies. In Evolutionary behavioral ecology (eds C Fox, DF Westneat), pp. 434-450. Cambridge, UK: Cambridge University Press.
106. Trivers RL. 1972 Parental investment and sexual selection. In Sexual selection and the descent of man (ed. B Campbell), pp. 136-179. Chicago, IL: Aldine Press.
107. Levitan DR, Petersen CW. 1995 Sperm limitation in the sea. Trends. Ecol. Evol. 10, 228-231. (doi:10. 1016/S0169-5347(00)89071-0)
108. Weddell N, Gage MJG, Parker GA. 2002 Sperm competition, male prudence and sperm-limited females. Trends. Ecol. Evol. 17, 313-320. (doi:10. 1016/S0169-5347(02)02533-8)
109. Mays HL, Albrecht T, Liu M, Hill GE. 2008 Female choice for genetic complementarity in birds: a review. Genetica 134, 147-58. (doi:10.1007/ s10709-007-9219-5)
110. Newcomer SD, Zeh JA, Zeh DW. 1999 Genetic benefits enhance the reproductive success of polyandrous females. Proc. Natl. Acad. Sci. USA 96, 10236-10241. (doi:10.1073/pnas.96.18.10236)
111. Eberhard WG. 1996 Females in control: sexual selection by cryptic female choice. Princeton, NJ: Princeton University Press.
112. Jones AG, Ardren WR. 2003 Methods of parentage analysis in natural populations. Mol. Ecol. 12, 2511-2523. (doi:10.1046/j.1365-294X. 2003.01928.x)
113. Bernasconi G, Keller L. 2001 Female polyandry affects their sons' reproductive success in the red flour beetle Tribolium castaneum. J. Evol. Biol. 14, 186-193. (doi:10.1046/j.1420-9101.2001.00247.x)
114. Byrne PG, Whiting MJ. 2008 Simultaneous polyandry increases fertilization success in an African foam-nesting treefrog. Anim. Behav. 76, 1157-1164. (doi:10.1016/j.anbehav.2008.05.019)
115. Byrne PG, Keogh JS. 2009 Extreme sequential polyandry insures against nest failure in a frog. Proc. R. Soc. B 276, 115-120. (doi:10.1098/rspb.2008.0794)
116. Foltz ADW, Schwagmeyer PL. 1989 Sperm competition in the thirteen-lined ground squirrel: differential fertilization success under field conditions. Am. Nat. 133, 257-265. (doi:10.1086/ 284914)
117. Kaitala A, Wiklund C. 1994 Polyandrous female butterflies forage for matings. Behav. Ecol. Sociobiol. 35, 385-388. (doi:10.1007/BF00165840)
118. Tregenza T, Wedell N. 1998 Benefits of multiple mates in the cricket Gryllus bimacculatus. Evolution 52, 1726-1730. (doi:10.2307/2411345)
119. Arnqvist G, Nilsson T. 2000 The evolution of polyandry: multiple mating and female fitness in insects. Anim. Behav. 60, 145-164. (doi:10.1006/ anbe.2000.1446)
120. Pearse DE, Janzen FJ, Avise JC. 2002 Multiple paternity, sperm storage, and reproductive success of female and male painted turtles (Chrysemys picta) in nature. Behav. Ecol. Sociobiol. 51, 164-171. (doi:10.1007/s00265-001-0421-7)
121. Murie J0. 1995 Mating behavior of Columbian ground squirrels. I. Multiple mating by females and multiple paternity. Can. J. Zool. 73, 1819-1926. (doi:10.1139/z95-214)
122. Simmons LW. 2001 The evolution of polyandry: an examination of the genetic incompatibility and good-sperm hypotheses. J. Evol. Biol. 14, 585-594. (doi:10.1046/j.1420-9101.2001.00309.x)
123. Burpee D, Sakaluk SK. 1993 Repeated matings offset costs of reproduction in female crickets. Evol. Ecol. 7, 240-250. (doi:10.1007/ BF01237742)
124. Ivy TM, Sakaluk SK, Url S. 2005 Polyandry promotes enhanced offspring survival in decorated crickets. Evolution 59, 152-159. (doi:10.1111/j.0014-3820. 2005.tb00902.x)
125. Ronkainen K, Kaitala A, Kivelä SM. 2010 Polyandry, multiple mating, and female fitness in a water strider Aquarius paludum. Behav. Ecol. Sociobiol. 64, 657-664. (doi:10.1007/s00265-009-0883-6)
126. Baer B, Schmid-Hempel P. 1999 Experimental variation in polyandry affects parasite loads and
fitness in a bumble-bee. Nature 397, 151-154. (doi:10.1038/16451)
127. Liu X-P, He H-M, Kuang X-J, Xue F-S. 2010 A comparison of female fitness between monogamy and polyandry in the cabbage beetle, Colaphellus bowringi. Anim. Behav. 79, 1390-1395. (doi:10. 1016/j.anbehav.2010.03.019)
128. Drnevich JM, Papke RS, Rauser CL, Rutowski RL. 2001 Material benefits from multiple mating in female mealworm beetles (Tenebrio molitor L.). J. Insect Behav. 14, 215-230. (doi:10.1023/A:1007889712054)
129. Svard L, MCNeil JN. 1994 Female benefit, male rick: polyandry in the true armyworm Pseudaletia unipuncta. Behav. Ecol. Sociobiol. 35, 319-326. (doi:10.1016/S0022-1910(98)00137-1)
130. McNamara KB, Elgar MA, Jones TM. 2008 A longevity cost of re-mating but no benefits of polyandry in the almond moth, Cadra cautella. Behav. Ecol. Sociobiol. 62, 1433-1440. (doi:10. 1007/500265-008-0573-9)
131. Uhl G, Schmitt S, Schäfer MA. 2005 Fitness benefits of multiple mating versus female mate choice in the cellar spider (Pholcus phalangioides). Behav. Ecol. Sociobiol. 59, 69-76. (doi:10.1007/s00265-005-0010-2)
132. Martin OY, Demont M. 2008 Reproductive traits: Evidence for sexually selected sperm. Curr. Biol. 18, R79 - R81. (doi:10.1016/j.cub.2007.11.031)
133. Myers EM, Zamudio KR. 2004 Multiple paternity in an aggregate breeding amphibian: the effect of reproductive skew on estimates of male reproductive success. Mol. Ecol. 13, 1951-1963. (doi:10.1111/j.1365-294X.2004.02208.x)
134. Wolf JB, Wade MJ. 2001 On the assignment of fitness to parents and offspring: whose fitness is it and when does it matter? J. Evol. Biol. 14, 347-356. (doi:10.1046/j.1420-9101.2001.00277.x)
135. Wade M. 1998 The evolutionary genetics of maternal effects. In Maternal effects as adaptations (eds T Mousseau, C Fox), pp. 5-21. Oxford, UK: Oxford University Press.
136. Jones AG, Walker D, Kvarnemo C, Lindström K, Avise JC. 2001 How cuckoldry can decrease the opportunity for sexual selection: data and theory from a genetic parentage analysis of the sand goby, Pomatoschistus minutus. Proc. Natl Acad. Sci. USA 98, 9151-9156. (doi:10.1073/pnas.171310198)
137. Shuker DM, Phillimore AJ, Burton-Chellew MN, Hodge SE, West SA. 2007 The quantitative genetic basis of polyandry in the parasitoid wasp, Nasonia vitripennis. Heredity 98, 69-73. (doi:10.1038/sj.hdy.6800897)
138. Halliday T, Arnold S. 1987 Multiple mating by females: a perspective from quantitative genetics. Anim. Behav. 35, 939-941. (doi:10.1016/S0003-3472(87)80138-0)
