

# Mate Choice and Sexual Selection

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BIO 666: Animal Behavior

Fall 2009

Northern Arizona University

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## The Presumed Importance of Female Mate Choice:

Mate choices influence female fitness through *direct selection* on females and through *indirect selection* on progeny



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## What is Direct Selection?

Selection on females that arises from variance in fitness *among females* due to differences in offspring numbers produced by different females.



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## What is Indirect Selection?



Selection on females that arises from variance in fitness *among offspring* due to mate choices made by different females.

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## Direct Selection on Choosy Females Is Presumed To:

Constrain sexual selection.

Mitigate sexual conflict.

Allow assessment of male resource or phenotypic quality.



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## Indirect Selection on Choosy Females Is Presumed To:



Constrain sexual selection.

Mitigate sexual conflict.

Allow assessment of male genetic quality.

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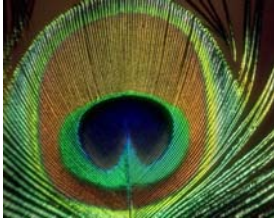
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## These Hypotheses Assume That:

Total selection on females is strong enough to counteract the effects of sexual selection on males.



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## Two Questions:

When *can* total selection on females constrain sexual selection on males?

When do the effects of male quality influence female fitness *most*?

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## What Do We Measure?

*The variance in fitness*; is proportional to the strength of selection.

*The sex difference in the variance in fitness*; its magnitude determines whether and to what degree the sexes will diverge.

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## What Tools Do We Use?

- The Opportunity for Selection.
- Analysis of Variance.



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## The Opportunity for Selection

Crow (1958, 1962)

$$I = V_w/W^2$$

Compares the fitness of breeding parents *relative* to the population before selection.

The variance in fitness,  $V_w$ , places *an upper limit* on the change in mean fitness from one generation to the next.

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## The Opportunity for Selection

Places an *upper limit* on phenotypic change because:

Heritability ( $h^2$ ) is usually less than 1.

The correlation between phenotypic change and fitness variance, i.e., the relationship between  $\Delta Z$  and  $V_w$  is usually less than 1.

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**How Can We Measure**  
 $I = V_w/W^2$   
**In a Natural Population?**



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**Begin with:**  
**The Mean and Variance**  
**in Offspring Numbers Among Females**

$$\bar{O} = \sum o_i / N_{females}$$

where  $o_i$  the brood size of the  $i$ -th female

$$V_O = \sum p_k (\bar{O} - o_i)^2$$

Where  $p_k$  = the proportion of females with brood size  $k$

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**Next:**  
**The Mean and Variance**  
**in Offspring Numbers Among Males**

Average Male Mating Success

$$= N_{females} / N_{males}$$

= the Sex Ratio ( $R$ )

$\bar{O}$  = Average Offspring/Female

$\bar{RO}$  = Average Offspring/Male

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**Like an ANOVA:  
The Distribution of Females with Males**

N Mates	Frequency	Mean # of Offspring	Variance in Offspring #
0	$p_0$	$0O$	$0V_o$
1	$p_1$	$1O$	$1V_o$
2	$p_2$	$2O$	$2V_o$
3	$p_3$	$3O$	$3V_o$
4	$p_4$	$4O$	$4V_o$
.	.	.	.
$k$	$p_k$	$kO$	$kV_o$
$N_{\text{♀♀}}$	1	$N_{\text{♀♀}}O$	$N_{\text{♀♀}}V_{o\text{♀♀}}$

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**A Key Point**

The mean and variance in offspring numbers for each mating class of males equals the products,  $jO$  and  $jV_{ofemales}$  respectively,

where  
 $j$  = harem size ;  $O$  = average offspring/female,  
 $V_{ofemales}$  = variance in offspring/female

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**This Means That:**

The mean and variance in offspring numbers among males will **far exceed** the mean and variance in offspring numbers among females.

Males with no mates will produce no offspring at all; thus unsuccessful males produce **fewer** offspring than the average female.

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**Like an ANOVA:  
The Distribution of Females with Males**

N Mates	Frequency	Mean # of Offspring	Variance in Offspring #
0	$p_0$	0O	$0V_o$
1	$p_1$	1O	$1V_o$
2	$p_2$	2O	$2V_o$
3	$p_3$	3O	$3V_o$
4	$p_4$	4O	$4V_o$
.	.	.	.
k	$p_k$	kO	$kV_o$
$N_{\text{♀♀}}$	1	$N_{\text{♀♀}}O$	$N_{\text{♀♀}}V_{o\text{♀♀}}$

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**As in ANOVA,**

$$V_{total} = V_{within} + V_{among}$$

= The *average of the variances* in offspring numbers within the classes of mating males  
+

The *variance of the averages* in offspring numbers among the classes of mating males

$$V_{males} = \sum p_j (jV_{Ofemales}) + \sum p_j (jO - RO)^2$$

$$= RV_{Ofemales} + O^2V_{mates}$$

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**The Total Opportunity  
for Selection on Males and Females**

(Wade 1979; Wade & Arnold 1980)

Recall that **RO** = average number of offspring/male;  
dividing  $V_{males}$  by  $[RO]^2$  gives

$$V_{males} / [RO]^2 = [RV_{Ofemales} + O^2V_{mates}] / [RO]^2$$

which gives

$$I_{males} = (1/R)I_{females} + I_{mates}$$

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## $I_{\text{mates}}$ Equals the *Sex Difference* in the Opportunity for Selection

$$I_{\text{males}} = 1/R (I_{\text{females}}) + I_{\text{mates}}$$

when  $R = 1$ ,

$$I_{\text{males}} - I_{\text{females}} = I_{\text{mates}}$$

In general, the *sex difference* in the opportunity for selection is due to *differences in mate numbers* between the sexes.

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## Conventional and Reversed Sex Roles

For species with *conventional* sex roles

$$I_{\text{♂}} = (1/R)I_{\text{♀}} + I_{\text{mates}}$$

For species with *reversed* sex roles

$$I_{\text{♀}} = (R)I_{\text{♂}} + I_{\text{mates}}$$

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## The Sex Difference in the Strength of Selection, $\Delta I$

$$\Delta I = \{ I_{\text{♂}} - I_{\text{♀}} \} = I_{\text{mates}}$$

When  $I_{\text{♂}} > I_{\text{♀}}$ , sexual selection modifies *males*

When  $I_{\text{♀}} > I_{\text{♂}}$ , sexual selection modifies *females*

When  $\Delta I = 0$ , either there is *no* sexual selection  
Or sexual selection is *equally strong*  
in both sexes

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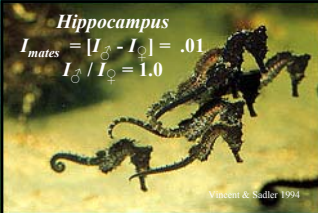
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**Hippocampus**  
 $I_{\text{mates}} = [I_{\sigma} - I_{\text{♀}}] = -.01$   
 $I_{\sigma} / I_{\text{♀}} = 1.0$



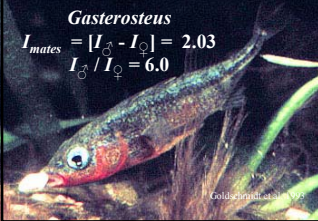
Vincent & Sadler 1994

**Syngnathus**  
 $I_{\text{mates}} = [I_{\sigma} - I_{\text{♀}}] = -.88$   
 $I_{\text{♀}} / I_{\sigma} = 5.4$




Berglund et al. 1989

**Gasterosteus**  
 $I_{\text{mates}} = [I_{\sigma} - I_{\text{♀}}] = 2.03$   
 $I_{\sigma} / I_{\text{♀}} = 6.0$



Goldstein et al. 1992

**Nerophis**  
 $I_{\text{mates}} = [I_{\sigma} - I_{\text{♀}}] = -1.04$   
 $I_{\text{♀}} / I_{\sigma} = 7.4$



Berglund et al. 1989

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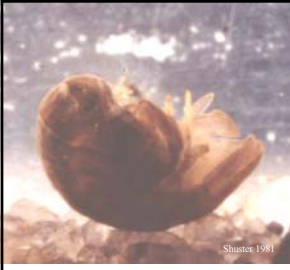
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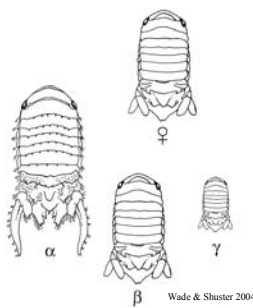
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Shuster 1981

**Paracerceis**  
 $I_{\text{mates}} = [I_{\sigma} - I_{\text{♀}}] = 2.8$   
 $I_{\sigma} / I_{\text{♀}} = 20.4$



Wade & Shuster 2004

**Thermosphaeroma**  
 $I_{\text{mates}} = [I_{\sigma} - I_{\text{♀}}] = 1.5$   
 $I_{\sigma} / I_{\text{♀}} = 4.5$

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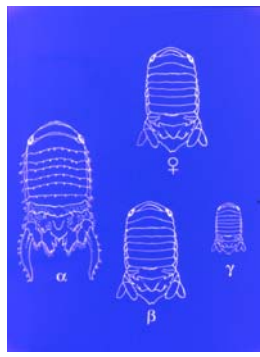
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**Paracerceis sculpta: A Worked Example**




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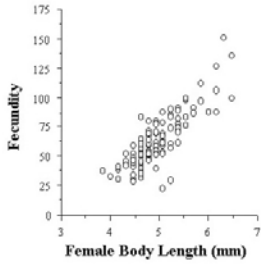
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## Calculating the Variance in Offspring Numbers for Females (N=825)



$$O_{\ominus} = 62.1$$

$$V_{O_{\ominus}} = 521.7$$

$$I_{\ominus} = V_{O_{\ominus}} / O_{\ominus}^2$$

$$= .14$$

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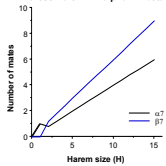
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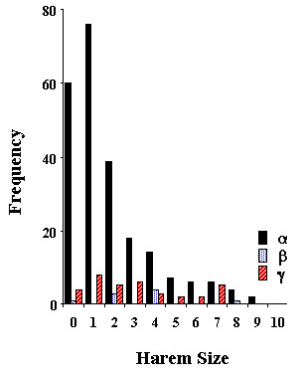
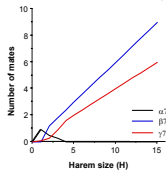
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## Some Rules for Assigning Male Mating Success

Fitness Rule #7: 1 alpha + 1 beta



Fitness rule #7c: 1 alpha+1 beta+1 gamma




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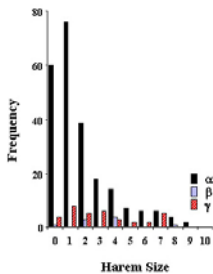
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## Calculating the Variance in Offspring Numbers for Each Morph



$$V_{O_{\ominus}total} = V_{O_{\ominus}within} + V_{O_{\ominus}among}$$

For the  $k$ -th male morph,

$$V_{O_{\ominus}k} =$$

$$\sum \sum p_{jk} (j_k V_{O_{\ominus}}) + \sum \sum p_{jk} (j_k O_{\ominus} - m_k O_{\ominus})^2$$

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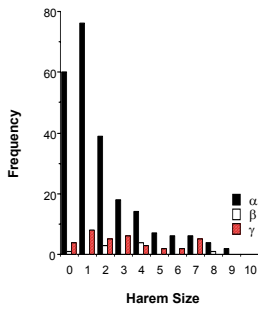
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## Calculating the Variance in Offspring Numbers for All Males (N=555)



$$V_{O\delta total} = V_{O\delta within} + V_{O\delta among}$$

$$= 24,488.0 + 20.6$$

$$(RO_{\delta})^2 = (92.6)^2 = 8,567.1$$

$$I_{\delta total} = 2.86$$

$$I_{\delta among} = .002$$

From Shuster & Wade 1991

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## How Much of Total Selection is Sexual Selection?

$$I_{\delta} = V_{O\delta} / (RO)^2 = 2.86$$

$$I_{\text{♀}} = V_{O\text{♀}} / O^2 = .14$$

$$I_{\delta} - I_{\text{♀}} = (1/R-1) I_{\text{♀}} + I_{\text{mates}}$$

$$I_{\text{mates}} = 2.77$$

$$I_{\text{mates}} / I_{\delta} = .97$$

$$I_{\delta} / I_{\text{♀}} = 20.4$$

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## This Means That:

Sexual selection in *P. sculpta* is so strong that direct selection on female fecundity is very small by comparison.




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## Conclusion I:

When can direct selection on females constrain sexual selection on males?



When sexual selection is *weak*.

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## Question Two:

When do the effects of *male quality* influence female fitness *most*?



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## The Sex Difference in the Opportunity for Selection

Recall that,

$$I_{males} - I_{females} = I_{mates}$$

To assess the effects of direct selection on females vs. sexual selection on males, we must measure

$$I_{females}$$

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## Recall That:

Direct selection on females affects the variance in offspring numbers among individuals.

Thus,  $I_{females}$  can be understood by investigating selection on female life history.

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## Three Components of Female Life History:

The number of times a female mates:

*Monandry vs. Polyandry*

The number of reproductive episodes in a female's lifetime:

*Semelparity vs. Iteroparity*

The duration of female reproductive competence:

*Uniseasonal vs. Multiseasonal Iteroparity*

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## The Effect of Monandry on $I_{mates}$

When a female mates *once* and produces only *one clutch* of offspring, she awards her *entire* reproductive output to a single male.



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### The Effect of Polyandry on $I_{\text{mates}}$

When a female mates *more than once*, she *partitions* her clutch into several sub-clutches, equal in number to the number of sires.



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### The Overall Effects of Polyandry on $I_{\text{mates}}$

Males sire *fewer* progeny with each female; because each mating male sires only a fraction of the offspring of each mate he secures, the variance in mate numbers among males is *reduced*.

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### The Effect of Semelparity on $I_{\text{mates}}$

When a female produces only *one clutch* of offspring, no variance exists *within females* in the number of offspring produced; all of the variance exists *among females*.



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## The Effect of Iteroparity on $I_{mates}$

When a female produces *more than one clutch*, the variance in offspring numbers can be partitioned into *within-* and *among-female* components.



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## The Overall Effects of Iteroparity on $I_{mates}$

Multiple reproductive episodes by females *erode*  $I_{mates}$  because as clutch number increases,  $I_{mates}$  becomes a smaller fraction of the total variance in offspring numbers.

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## This Means That:

$I_{mates}$  is eroded *least* in monandrous, semelparous species, and is eroded *most* in polyandrous, iteroparous species.



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## The Opportunity for Selection on Female Life History

Wade (1987)

$$I_{clutches} = V_{clutches} / X^2_{clutches}$$

$I_{clutches}$  is the opportunity for selection on females arising from multiple matings and from multiple reproductive events.

Both tendencies simultaneously *decrease* the variance in fitness among males and *increase* the variance in fitness among females.

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## The Total Opportunity for Selection

Wade (1987)

$$I_{males} = 1/R (I_{females} - I_{clutches}) + I_{mates}$$

$I_{clutches}$  equals the opportunity for selection on females, owing to variance among females in the number of clutches produced.

$I_{mates}$  equals the sex difference in the opportunity for selection.

When the sex ratio,  $R$ , is assumed to equal 1

$$I_{males} - I_{females} = I_{mates} - I_{clutches}$$

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## How Can We Measure $I_{clutches}$ in a Natural Population?



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## Measuring the Variance in Offspring Numbers Among Females

### Approach 1: Two Factor ANOVA

Identifies main effects of male and female parents as well as effects of parental interactions on offspring numbers.

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## Measuring the Variance in Offspring Numbers Among Females

### Approach 2: Nested ANOVA

The effects of males and females are not considered fixed, but instead represent a *random* selection from the breeding population.

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Table 4.1. Breeding design for females that mate more than once and produce more than one clutch of offspring with each mate; sperm are not stored after the last oviposition with each mate.

Females (a=3)	F <sub>1</sub>			F <sub>2</sub>			F <sub>3</sub>		
Males (b=3)	M <sub>11</sub>	M <sub>12</sub>	M <sub>13</sub>	M <sub>21</sub>	M <sub>22</sub>	M <sub>23</sub>	M <sub>31</sub>	M <sub>32</sub>	M <sub>33</sub>
Clutches (n=3)	C <sub>111</sub>	C <sub>112</sub>	C <sub>113</sub>	C <sub>211</sub>	C <sub>212</sub>	C <sub>213</sub>	C <sub>311</sub>	C <sub>312</sub>	C <sub>313</sub>
	C <sub>112</sub>	C <sub>122</sub>	C <sub>132</sub>	C <sub>212</sub>	C <sub>222</sub>	C <sub>232</sub>	C <sub>312</sub>	C <sub>322</sub>	C <sub>332</sub>
	C <sub>113</sub>	C <sub>123</sub>	C <sub>133</sub>	C <sub>213</sub>	C <sub>223</sub>	C <sub>233</sub>	C <sub>313</sub>	C <sub>323</sub>	C <sub>333</sub>
Sire sums $\sum C_{ijk}$	C <sub>11</sub>	C <sub>12</sub>	C <sub>13</sub>	C <sub>21</sub>	C <sub>22</sub>	C <sub>23</sub>	C <sub>31</sub>	C <sub>32</sub>	C <sub>33</sub>
Sire means $C_{i.}$	C <sub>011</sub>	C <sub>012</sub>	C <sub>013</sub>	C <sub>021</sub>	C <sub>022</sub>	C <sub>023</sub>	C <sub>031</sub>	C <sub>032</sub>	C <sub>033</sub>
Dam means $C_{.j}$	C <sub>01</sub>	C <sub>02</sub>	C <sub>03</sub>	C <sub>01</sub>	C <sub>02</sub>	C <sub>03</sub>	C <sub>01</sub>	C <sub>02</sub>	C <sub>03</sub>

$$\text{Grand mean } (C_{000}) = (1/abn) \sum \sum \sum C_{ijk}$$

$$SS_{\text{among}} (\text{among groups}) = ab \sum (C_{i.} - C_{000})^2$$

$$SS_{\text{dams}} (\text{sires within dams}) = a \sum \sum (C_{.j} - C_{000})^2$$

$$SS_{\text{dams}} (\text{within dams}) = \sum \sum \sum (C_{ijk} - C_{i.})^2$$

#### Sources of Variance in Offspring Numbers:

*V<sub>within</sub>* = variance in clutch size within females (SS<sub>dams</sub> divided by a(b-1) = MS<sub>1</sub>)

*V<sub>sires</sub>* = variance in clutch size due to individual mating males (SS<sub>dams</sub> divided by a(b-1) = MS<sub>2</sub>)

*V<sub>among</sub>* = variance in clutch size among females (SS<sub>among</sub> divided by (a-1) = MS<sub>3</sub>)

MS<sub>2</sub> / MS<sub>1</sub> = the effect of individual females on offspring numbers

MS<sub>3</sub> / MS<sub>1</sub> = the effect of individual sires on offspring numbers

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## The Variance Components of $V_{females}$

$$V_{females} = V_{clutch\ number} + V_{sires\ within\ females} + V_{clutch\ size}$$

$V_{clutch\ number}$  = the variance in offspring numbers arising from females' production of multiple clutches of offspring.

$V_{sires\ within\ females}$  = the variance in offspring numbers arising from the effects of multiple sires.

$V_{clutch\ size}$  = the variance in average number of offspring per clutch, calculated across all females, i.e., the *among-female* component of variance in offspring numbers.

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## The Variance Components of $V_{females}$

$V_{clutch\ number} + V_{sires\ within\ females}$  = the variance in offspring numbers, averaged across all females, that is, the *within-female* component of variance in offspring numbers.

$$\text{If } V_{clutches} = V_{clutch\ number} + V_{sires\ within\ females},$$

then because ,

$$V_{females} = V_{clutch\ number} + V_{sires\ within\ females} + V_{clutch\ size}$$

$$V_{females} = V_{clutches} + V_{clutch\ size} \text{ or}$$

$$V_{clutch\ size} = V_{females} - V_{clutches}$$

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## The Relationship of $V_{females}$ to $I_{clutches}$

$$V_{clutch\ size} = V_{females} - V_{clutches}$$

Then if each of these terms is divided by the square of the grand mean in offspring per female,

$$I_{clutch\ size} = I_{females} - I_{clutches}$$

Recall that the total opportunity for selection is,

$$I_{males} = 1/R (I_{females} - I_{clutches}) + I_{males}$$

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## This Means That:

Nested ANOVA provides a method for measuring the effects of multiple sires and multiple breeding episodes on  $I_{females}$  that is consistent with Wade (1987).




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## However, Recall That:

$$I_{males} = \frac{1}{R} [I_{females} - (I_{clutch\ number} + I_{sires\ within\ females})] + I_{mates}$$

If the effects of male “quality” lie *within*  $I_{sires\ within\ females}$ , which lies *within*  $I_{clutches}$ , then in most species,

$$I_{sires\ within\ females} < I_{clutches} < I_{females} < I_{mates}$$

↑ ↑ ↑  
*Indirect Selection*    *Direct Selection*    *Total selection on females*

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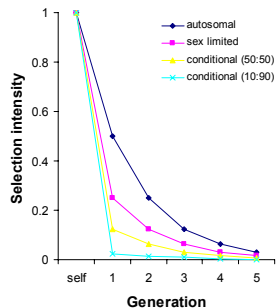
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## Indirect Selection Occurs Across Generations

The intensity of indirect selection *diminishes* by ½ with each generation.

Indirect selection intensity on sex limited traits is *further* diminished.

Indirect selection on conditional traits is diminished *further still*.




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## When Female Mate Choice Occurs:

Few males produce each generation;  $I_{\text{mates}}$  becomes *extremely large* compared to the opportunity for selection on females,  $I_{\text{females}}$ .  
When this happens,  $I_{\text{clutches}}$  and  $I_{\text{sires within females}}$  become *extremely small*.

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## Conclusion II:



When do the effects of male quality influence female fitness *most*?

When sexual selection is *negligible*.

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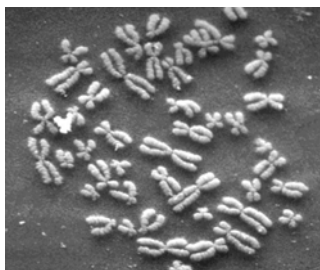
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## Sexual Selection in Humans

Sex-differences in *genetic drift* creates different patterns of genetic diversity for genes inherited through each sex.



**Prediction:** Genetic diversity will *decrease* with *increasing* selection intensity.

**Test:** Y chromosome and mitochondrial sequence divergence in *Homo sapiens*

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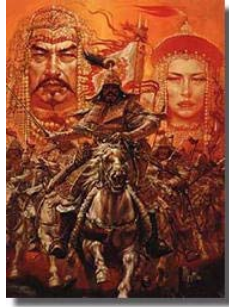
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## An Example of Low Y-Chromosome Diversity

Nearly 8% of the men living in the region formerly controlled by the Mongol Empire

**Share the same** 1,000 year old Y-chromosome haplotype originating in Mongolia.



This is approximately 1.0% of the world's human population.

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**For Other Human Populations:**  
Sexual selection represents an average of 54.8% (range 28.4% to 77.7%) of all selection

**Sexual selection in human populations has the potential to be very strong.**

THE MONGOL EMPIRE

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**Facial Symmetry Indicates 'Genetic Quality?'**

But recall that selection on 'quality' is strongest when  $I_{mates} = 0$ .

Adaptive benefits in this context may be **unlikely** to the extent to which human populations have experienced sexual selection.

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## Is Facial Symmetry Really Attractive

Not all symmetrical faces are “beautiful.”

A possible explanation is that human facial perception is tuned to “directional symmetry” which provides information in social situations.

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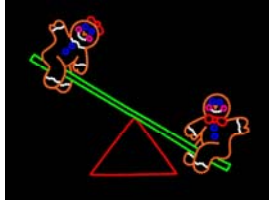
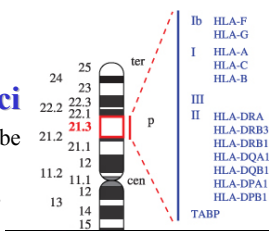
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## Major Histocompatibility Complex (MHC) Loci

Sequence variability appears to be involved in olfactory mate attraction in fish, mice, humans; choices favor **heterozygosity**.

**Interpretation:** particular combinations may be ‘uniquely compatible’.

However, such **balancing selection** is unlikely to generate directional change.




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## In General:



Male quality will be **least important** to females when  $I_{mates}$  is extremely large compared to  $I_{clutches}$ ; at such times, female preferences are likely to be **arbitrary**.

Male quality will be **most important** when  $I_{mates}$  and  $I_{clutches}$  are approximately equal in magnitude; such mating systems may be **unstable**.

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